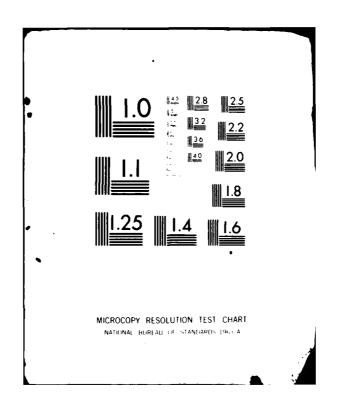
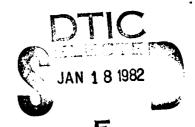
PENNSYLVANIA STATE UNIV UNIVERSITY PARK APPLIED RESE--ETC F/6 17/1 EFFECTS OF PHASE CANCELLATION ON THE SCATTERING MEASUREMENTS. (U) JUL 81 J N DZIERZANOWSKI N00024-79-C-6043 ARL/PSU/TM-81-201 ML AD-A109 682 UNCLASSIFIED 100 Z Ą ı





EFFECTS OF PHASE CANCELLATION ON THE SCATTERING MEASUREMENTS

James M. Dzierzanowski



Technical Memorandum File No. TM 81-201 July 1, 1981 Contract No. NO0024-79-C-6043

Copy No. 5

The Pennsylvania State University Intercollege Research Programs and Facilities APPLIED RESEARCH LABORATORY Post Office Box 30 State College, PA 16801

NAVY DEPARTMENT

NAVAL SEA SYSTEMS COMMAND

0 1 15 82 048

DIE MIE COPY

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE

1. REPORT NUMBER	2 COUT ACCESSION NO	3. RECIPIENT'S CATALOG NUMBER
TM 81-201	AD-A1096821	S. RECIFIENT S CATALOG NUMBER
4. TITLE (and Subtitle)	11000	5. TYPE OF REPORT & PERIOD COVERED
EFFECTS OF PHASE CANCELLATION ON MEASUREMENTS	THE SCATTERING	M.S. Thesis, August 1981
		6. PERFORMING ORG. REPORT NUMBER TM 81-201
7. AUTHOR(s)		8. CONTRACT OR GRANT NUMBER(s)
James M. Dzierzanowski		NOOO24-79-C-6043
9. PERFORMING ORGANIZATION NAME AND ADDRESS	<u> </u>	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
The Pennsylvania State Universi	•	
Applied Research Laboratory, P. State College, PA 16801	О. ВОХ 30	
11. CONTROLLING OFFICE NAME AND ADDRESS		12. REPORT DATE
Naval Sea Systems Command)	July 1, 1981
Department of the Navy]	13. NUMBER OF PAGES
Washington, DC 20362	from Controlline Office)	101 pages and figures 15. SECURITY CLASS. (of this report)
		•
		Unclassified, Unlimited
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE
17. DISTRIBUTION STATEMENT (of the abstract entered i	n Block 20, il dillereni Iron	n Report)
19. KEY WORDS (Continue on reverse side if necessary and	identify by black number)	
thesis, phase, cancellation, scat		ents
1		
!		
20. ABSTRACT (Continue on reverse side if necessary and		
Piezoelectric transducers are and acoustic energy in such diversif acoustic propagation, and non-destruducer when used as a receiver is senwave. The effect of phase cancellat coefficients of heterogeneous materistudied extensively. However, the f	used for convertied fields as medictive material to sitive to the phasion on the measurals with piezocle	dical imaging, underwater esting. This type of transasse of the received pressure rements of attenuation ectric transducers has been
P FORM 1479		

DD 1 JAN 73 1473 EDITION OF 1 NOV 65 IS OBSOLETE

UNCLASSIFIED

READ INSTRUCTIONS BEFORE COMPLETING FORM

SECURITY CLASSIFICATION OF THIS PAGE(When Date Entered)

/also produce considerable error in scattering measurements has only recently been recognized.

In this thesis, a mathematical model for interpretation of error arising from the phase cancellation effect on backscattered waves is developed. Computer simulation has been performed to elucidate the influence of phase cancellation on the average received pressure in terms of transducer aperture size, number of scatterers, target range and frequency for five different scattering configurations; a single point scatterer; linear, rectangular and random arrays; and random volume distributions of point scatterers.

Accession F	or
NTIS GRA&I	×
DTIC TAB	
Unannounced	
Justificati	.on
Py. Distribut Avet	n/ De Codes
: .	d/or
Dist · :	·. 41
A	

Piezoelectric transducers are used for converting between electrical and acoustic energy in such diversified fields as medical imaging, underwater acoustic propagation, and non-destructive material testing. This type of transducer when used as a receiver is sensitive to the phase of the received pressure wave. The effect of phase cancellation on the measurements of attenuation coefficients of heterogeneous materials with piezoelectric transducers has been studied extensively. However, the fact that the phase cancellation effect may also produce considerable error in scattering measurements has only recently been recognized.

In this thesis, a mathematical model for interpretation of error arising from the phase cancellation effect on backscattered waves is developed. Computer simulation has been performed to elucidate the influence of phase cancellation on the average received pressure in terms of transducer aperture size, number of scatterers, target range, and frequency for five different scattering configurations; a single point scatterer; linear, rectangular and random arrays; and random volume distribution of point scatterers.

Results of the computer simulation demonstrate that judicious choice of transducer aperture, target range, and operating frequency is necessary to minimize artifact induced by the phase cancellation effect. Based on a maximum 10% error, aperture values of .75 cm or less, farfield target range and frequency range of 1.00 to 15.00 megahertz should be employed when implementing phase-sensitive transducers as receivers.

TABLE OF CONTENTS

		Page
	Abstract	iii
	List of Figures	v
	Acknowledgments	ix
СНАРТЕ	<u>R</u>	
I.	INTRODUCTION	. 1
II.	FORMULATION OF THE PROBLEM	. 5
III.	RESULTS AND DISCUSSION	11
	Single Point Scatterer	11
	Linear Scatterer Array	31
	Rectangular and Randomly-Distributed Scatterers	34
	Random Volumetric Distribution	48
IV.	SUMMARY AND CONCLUSIONS	50
	REFERENCES	56
	APPENDIX A: Histogram of Average Received Pressure	57
	APPENDIX B: How To Use The Computer Programs	66

LIST OF FIGURES

Figure			Page
1.	Geometrical configuration of the scattering arrangements		6
2.	Four scattering arrangements which are studied are graphically illustrated	•	10
3.	Phase-cancellation at the transducer surfaces of different size due to a spherical wave generated by a single scatterer located at the center of the incident beam	•	12
4.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .10 cm in diameter situated at $10.00~\rm cm$ away from the transducer	•	13
5.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .25 cm in diameter situated at $10.00~\rm cm$ away from the transducer	•	14
6.	Computed normalized pressure amplitude distribution on the face of a $5.00~\mathrm{MHz}$ transducer of .50 cm in diameter situated at $10.00~\mathrm{cm}$ away from the transducer	•	15
7.	Computed normalized pressure amplitude distribution on the face of a $5.00~\mathrm{MHz}$ transducer of .75 cm in diameter situated at $10.00~\mathrm{cm}$ away from the transducer	•	16
8.	Computed normalized pressure amplitude distribution on the face of a $5.00~\mathrm{MHz}$ transducer of $1.00~\mathrm{cm}$ in diameter situated at $10.00~\mathrm{cm}$ away from the transducer	•	17
9.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of 1.25 cm in diameter situated at 10.00 cm away from the transducer	•	18
10.	Two-dimensional normalized phase distribution on the face of a 5.00 MHz transducer of .75 cm in aperture at a target range of 10.00 cm	•	20
11.	Two-dimensional normalized amplitude distribution on the face of a 5.00 MHz transducer of .75 cm in aperture at a target range of 10.00 cm	•	21
12.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .50 cm in diameter at a target range of 5.00 cm		23

Figure		Pag	<u>;e</u>
13.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .50 cm in diameter at a target range of 7.50 cm	. 24	ţ
14.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .50 cm in diameter at a target range of 10.00 cm	. 25	;
15.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .50 cm in diameter at a target range of 12.50 cm	. 26	;
16.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .50 cm in diameter at a target range of 15.00 cm	. 27	,
17.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .50 cm in diameter at a target range of 20.00 cm	. 28	3
18.	Average received pressure measured by transducers of .25, .50, .75, 1.00, 1.25, and 1.50 cm in diameter due to a scatterer is plotted versus the range of the system at 5.00 MHz	. 29)
19.	Average received pressure measured by transducers of .10, .25, .50, .75, 1.00, and 1.25 cm in diameter due to a scatterer located 20.00 cm away is plotted versus frequency of the wave	. 30)
20.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of 1.00 cm in diameter due to a linear array of 25 scatterers located 20.00 cm away from the transducer	. 32	2
21.	Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of 1.00 cm in diameter due to a linear array of 100 scatterers located 20.00 cm away from the transducer	. 33	;
22.	Average received pressure measured by transducers of .25, .50, .75, 1.00, and 1.25 cm in diameter at 5.00 megahertz and at a range of 15.00 cm versus the number of scatterers	. 35	, I
23a.	Average received pressure measured by transducers of .25, .50, .75, and 1.00 cm in diameter at 5.00 megahertz and at a range of 20.00 cm versus the number of scatterers	. 37	•

Figure	·	Page
23b.	Average received pressure measured by transducers of .25, .50, .75, and 1.00 cm in diameter at 5.00 megahertz and at a range of 20.00 cm versus the number of scatterers	. 38
24.	Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of .50 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer	. 39
25.	Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of .75 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer	. 40
26.	Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of 1.25 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer	. 41
27.	Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of .50 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer	. 42
28.	Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of .75 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer	. 43
29.	Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of 1.25 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer	. 44
30.	Average received pressure measured by transducers of .25, .50, .75, 1.00, and 1.25 cm due to 200 scatterers arranged in a rectangular distribution at 5.00 megahertz versus range	. 46
31.	Average received pressure measured by transducers of .10, .25, .50, .75, and 1.00 cm in diameter due to 200 scatterers at a range of 20.00 cm versus frequency	. 47
32.	Average received pressure measured by a .25 cm transducer at a range of 15.00 cm with a frequency of 5.00 megahertz versus the number of scatterers	. 49
33.	Average received pressure versus R/D for the random planar distribution	. 52

Figure				Page	:
34.	Average received pressure measured by transducers of .25, .50, .75, 1.00, 1.25, and 1.50 cm in diameter versus R/F for the random planar distribution			. 53	
35.	Average received pressure versus $R\lambda/D$ for the random planar distribution	•		. 54	
36.	Average received pressure versus the number of occurrences for a single point scatterer at a range of 7.50 cm and aperture of .50 cm over 25 trials			. 59	
37.	Average received pressure versus the number of occurrences for a single point scatterer at a range of 7.50 cm and aperture of .75 cm over 25 trials	•	•	. 60	
38.	Average received pressure versus the number of occurrences for a single point scatterer at a range of 7.50 cm and aperture of 1.00 cm over 25 trials			. 61	
39.	Average received pressure versus the number of occurrences for a single point scatterer at a range of 7.50 cm and aperture of 1.25 cm over 25 trials			. 62	
40.	Average received pressure versus the number of occurrences for 200 scatterers at a range of 20.00 cm and aperture of .50 cm over 25 trials	•	•	. 63	
41.	Average received pressure versus the number of occurrences for 200 scatterers at a range of 20.00 cm and aperture of .75 cm over 25 trials	•		. 64	
42.	Average received pressure versus the number of occurrences for 200 scatterers at a range of 20.00 cm and aperture of 1.00 cm over 25 trials	•	•	. 65	
43.	Sample input to program PHASE			. 67	

ACKNOWLEDGMENTS

The author gratefully acknowledges the continued support and direction of Dr. K. Kirk Shung. The author also wishes to acknowledge the staff of the Hybrid Computer Laboratory, Mr. Adam D. Savakus and Mr. Alan J. Snyder for the assistance they have provided in this work.

This work was supported by The Pennsylvania State University, Applied Research Laboratory under contract with the U.S. Naval Sea Systems Command and NSF grant DAR 80-18415.

CHAPTER I

INTRODUCTION

Sound is a mechanical wave which can be produced by an object vibrating in a medium, such as air, water, metal, or tissue. Sound waves have been found extremely useful in such diversified fields as medical imaging, non-destructive material testing and underwater warfare. Ultrasound refers to sound waves above the frequency of human hearing (approximately 20 kilohertz). It is sensitive to density and structural variations in biological tissue and materials. In the case of ultrasonic medical imaging, in vivo measurements are possible without harmful side effects of ionizing radiation, such as X-rays. Similarly, ultrasonic material evaluation for flaw detection and fatigue can be performed without actual destruction of the material during the testing procedure. Fundamentally, scattering and reflection of sound waves occurs if there is a mismatch of acoustic propagation properties such as velocity, density, and compressibility between two media. The reflected or scattered sound waves are detected and electronically processed to provide information regarding the dimensions and locations of nonuniformities within the interrogated material. Overall, the success of utilizing sound waves as a medium for investigation purposes lies within the non-destructive nature of sound and its sensitivity to changes in elastic properties of the material on a level significant to imaging requirements. In some applications, sound is generated by electrically exciting a piezoelectric crystal such as quartz or Lead Zirconate Titanate (PZT).

The piezoelectric transducer, when used as a receiver of sound waves, however, is sensitive to the phase of the impinging sound wave. This phase sensitive nature of the piezoelectric transducer may give rise to serious consequences in situations involving the determinations of acoustic propagation parameters such as attenuation and scattering of inhomogeneous materials. This is basically due to the non-uniformness of the wavefront of the scattered wave or waves which have traversed through heterogeneous materials arriving at the face of a finite-aperture transducer. This fact implies that the phase differences among wavelets arriving at different areas of the transducers surface may be significant enough that signal cancellation results.

The artifact caused by the phase-sensitive nature of the piezoelectric receivers which is termed the phase cancellation effect in the attenuation measurements of an inhomogeneous medium was first addressed by Marcus and Carstensen (1975). Their work indicated a good correlation between the relative degree of sample inhomogeneity and the magnitude of the absorption error, as measured by a conventional phase-sensitive receiver. Marcus and Carstensen experimentally compared a radiation force known as an acoustic-electric receiver (AET) with a conventional piezoelectric receiver (PIT) for the measurement of the absorption coefficient of various homogeneous and inhomogeneous materials. For 2% agar samples, an acoustically uniform material, the attenuation measured by both types of transducers proved similar. However, for beef muscle, an acoustically inhomogeneous tissue, attenuation values differed. For measurements at 2.00 megahertz, the piezoelectric receiver had absorption coefficients ranging from 0.21 to 1.15 nepers/cm, whereas a radiation force receiver measured 0.21 to

0.24 nepers/cm. The wide range of absorption values measured by a piezoelectric transducer was attributed to the phase cancellation artifact on the surface of the receiving piezoelectric element. They, therefore, suggested the use of a phase-insensitive acoustic-electric receiver in this type of measurement.

Further work by Busse and Miller (1976) substantiated the existence of phase cancellation effects, noting the influence of transducer aperture on absorption measurements (indicating that a reduction of phase cancellation error is possible with a decrease in transducer aperture) and experimentally compared the PZT and AET. The AET, utilizing a cadmium sulfide crystal, virtually eliminated the phase cancellation effect arising from structurally inhomogeneous tissue specimens. This transducer was sensitive to the total power of the incident acoustic wave, not the impinging phasefront. Heyman (1979) investigated the effects of phase cancellation on inhomogeneous material characterization (largely anisotropic stressed metal samples) by PZT and AET and found a notable difference in the attenuation measurements. Furthermore, materials with irregular flatness and parallelism also influence the degree of phase cancellation.

Reid, Shung, and Kak (1979) have expanded the concept of phase cancellation to include scattered or reflected waves. Data for scattered waves*showed that the scattered strength per unit volume of scatterers of dilute polysterene spheres, suspended in mixed solution of water and glycerine and measured with a piezoelectric transducer of 1.00 cm in diameter located 16.00 cm from the scatterers, is 1.7 dB lower than that obtained with a piezoelectric transducer of smaller diameter (0.635 cm).

In this thesis errors which may be introduced due to the phase cancellation artifact in backscattering measurements are examined based on computer simulation of the experimental process. Parameters of interest include transducer aperture, number of scatterers, distance between the transducer and scattering medium, and frequency. The pressure received by the transducer is compared to a small microprobe with a diameter of 1.0 mm which can be approximated as a point receiver in the lower megahertz range. This investigation also includes varied scattering arrangements. The first and simplest case is a single point scatterer located at the center of the ultrasonic beam profile. This arrangement is useful for two reasons: the effect of path length differences on the phase of the pressure wave between the center and edges of the transducer are readily apparent and computations are greatly simplified. The second scattering arrangement is a linear array, or a single line of point scatterers extending from one edge of the transducer to the opposite edge. Rectangular and random two-dimensional arrangements of point scatterers distributed over a plane parallel to the transducer face are other configurations modelled. These two configurations, along with a random volume arrangement, more closely approximate the experimental acoustic backscattering arrangements.

FORMULATION OF THE PROBLEM

To facilitate computation, the transducer aperture is divided into N elements, which are small enough so that the pressure received by element n can be represented by the pressure received at the center of the small element (point n), as shown in Figure 1. Assuming that the incident wave is a monochromatic plane wave, we have:

$$P_i$$
 = incident pressure at scatterer j
= $P(0)e^{ikR}j$ [1]

where k is the wave number (radians/cm), P(0) is the pressure transmitted by the transducer and R_j is the distance along the axis perpendicular to the transducer face to scatterer j within the volume.

For conversion from the three-dimensional case as presented in Figure 1 to the two-dimensional case, let $R_j=R$, where R is the target range, or let L, the thickness of the scattering volume, approach zero. The scatterers would then be placed within the plane rather than in the scattering volume. Introducing the condition $R>D^2/\lambda$, where D is the diameter of the scatterers and λ is the wavelength, the scattered wave, P_{nj} , at point n on the transducer face due to a scatterer j within the scattering volume, can be approximated by the following equation:

$$P_{nj} = P_i \frac{S_j(\hat{o}, \hat{i})}{r_{nj}} e^{ik(r_{nj})}$$
 [2]

where $S_j(\hat{o},\hat{i})$ is the scattering amplitude function of the jth scatterer and \hat{o},\hat{i} are unit vectors representing observation and incident directions,

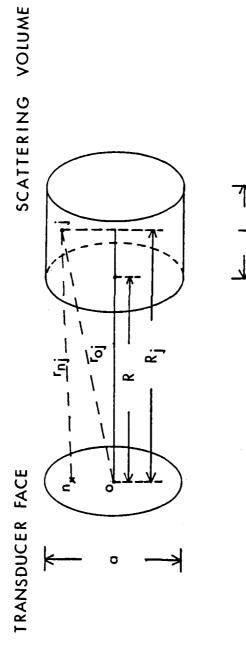


Figure 1. Geometrical configuration of the scattering arrangements.

respectively. Substituting P_i from equation [1] into equation [2] yields:

$$P_{nj} = \frac{P(0) S_{j}(\hat{0}, \hat{1})}{r_{nj}} e^{ik(R_{j}+r_{nj})}$$
 [3]

Similarly the scattered wave at the center of the transducer face, point o, due to the scatterer j, P_{oj} is given by:

$$P_{oj} = \frac{P(0) S_{j}(\hat{o}, \hat{1})}{r_{oj}} e^{ik(R_{j} + r_{oj})}$$
[4]

 P_{oj} will be simultaneously developed with P_{nj} for use as a reference (this will be elaborated in several steps). If kD>>1, we can further assume that scatterers within the scattering volume are identical point scatterers and are at rest within the scattering arrangement. For identical point scatterers, $S_{j}(\hat{o},\hat{1})$ is a constant independent of \hat{o} and $\hat{1}$, therefore $S_{j}(\hat{o},\hat{1})=s$.

$$P_{nj} = \frac{P(0)s}{r_{nj}} e^{ik(R_j + r_{nj})}$$
 [5]

and

$$P_{oj} = \frac{P(0)s}{r_{oj}} e^{ik(R_j + r_{oj})}$$
 [6]

Here a single scattering process is assumed. The assumptions generally hold if the scatterer concentration is low and kD>>1. Now further assuming R>>a (a is diameter of the transducer aperture) and R>>L (L is the thickness of the scattering volume), $r_{nj} \approx r_{oj} \approx R$. However,

this approximation is not applicable to the phase term because very small changes in path lengths produce substantial phase variation. We thus obtain:

$$P_{nj} = \frac{P(0)s}{R} e^{ik(R_j + r_{nj})}$$
 [7]

and

$$P_{0j} = \frac{P(0)s}{R} e^{ik(R_j + r_{0j})}$$
 [8]

As previously stated, the intention of this thesis is to elucidate the phase cancellation effect on the transducer aperture. This is accomplished by expressing the average received pressure as determined by finite-aperture transducers in terms of pressure received by a point receiver located at point o, therefore P_{nj} is normalized with respect to P_{oj} . In this way, the phase at point o is used as reference and only the relative phase difference between point n and point o is considered, i.e.,

$$P_{nj}/P_{oj} = e^{ik(r_{nj}-r_{oj})}$$

$$= e^{i\theta}nj$$
[9]

The phase value at the center becomes 0.0 degrees as a result of this normalization process and as a consequence, the calculated phase value over a certain point on the transducer face indicates the phase of the wave at that point relative to the center of the transducer.

If there are M scatterers in the scattering volume, the average received pressure $P_{\rm ave}$ received by the transducer is then given by:

$$P_{\text{ave}} = \frac{1}{N} \sum_{n=1}^{N} \sum_{j=1}^{M} e^{i\theta} nj$$

$$= Pe^{i\theta}$$
[10]

where P, θ are the magnitude and phase of Pave.

The amplitude of the average pressure AMP can be obtained by taking the real part of $\mathbf{P}_{\mathbf{ave}}$:

$$AMP = Real(Pe^{i\theta})$$
 [11]

Figure 2 depicts the first four scattering arrangements used in the computer model. The particle dimension in this figure is exaggerated for the sake of illustrating the scattering configurations. Although not depicted here, the random volumetric arrangement is similar to the random planar distribution, except that the scatterers are randomly dispersed within a cylinder of thickness L.

In the computer model, N, the number of elements representing the transducer surface area, is assigned a value of 431.

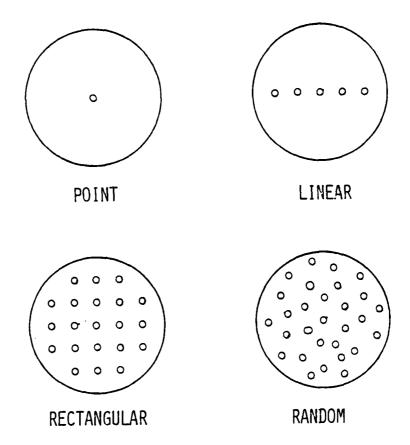


Figure 2. Four scattering arrangements which are studied are graphically illustrated.

RESULTS AND DISCUSSION

The results and discussion are presented in the following according to the five scattering configurations studied.

Single Point Scatterer

The significance of a physical phenomenon can usually be revealed more readily with simple examples. Therefore, this study included the simplest scattering arrangement possible, depicted in Figure 3, which shows a spherical wave originated from a scatterer located at the center of the ultrasonic beam impinging upon circular transducers with aperture sizes of A_1 and A_2 . It becomes readily apparent from this figure that the phase differences θ_1 and θ_2 between waves arriving at the center and the edge of the transducers depend upon the aperture size of the transducer and the target range was well as the frequency of the wave. These are the three parameters which have been investigated for this case.

Figures 4 through 9 show the three-dimensional normalized amplitude distribution across the transducer face for apertures of .10, .25, .50, .75, 1.00, and 1.25 cm at a frequency of 5.00 megahertz and range of 10.00 cm. Figure 4 establishes that the pressure amplitude over a transducer with an aperture of 1.00 mm in diameter is virtually constant. Therefore, the phase cancellation effect for transducers with small apertures is negligible. It will be seen later on that this statement holds for all scattering configurations studied. This is

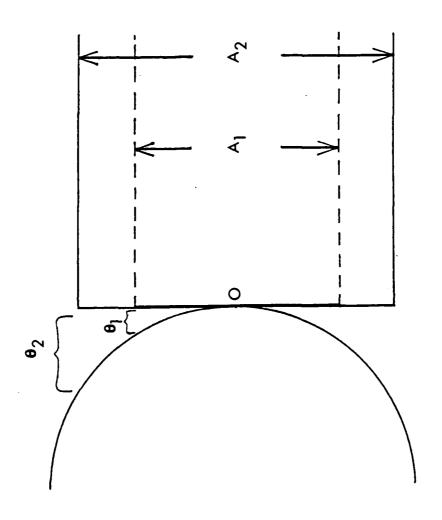
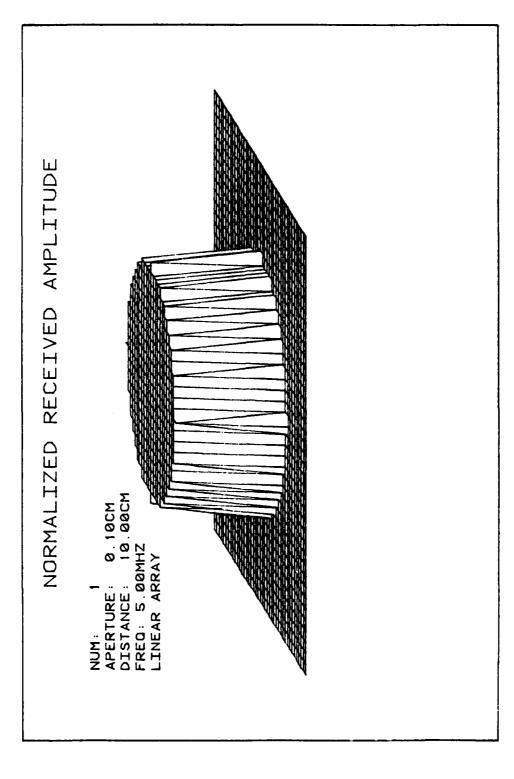
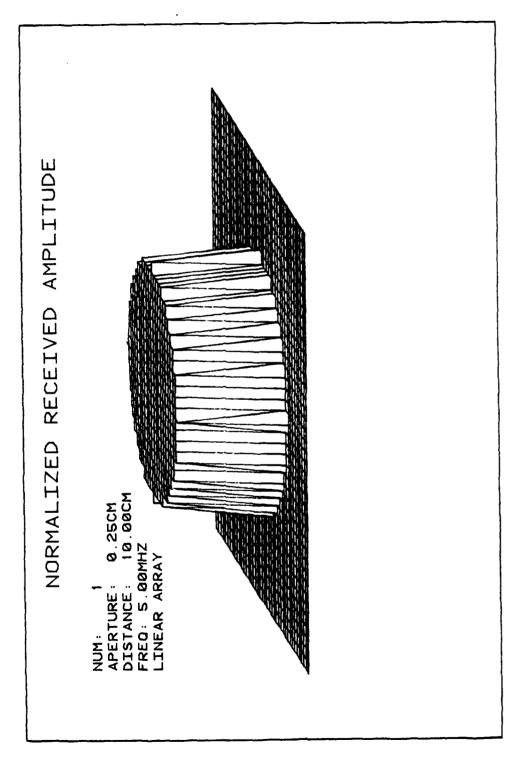


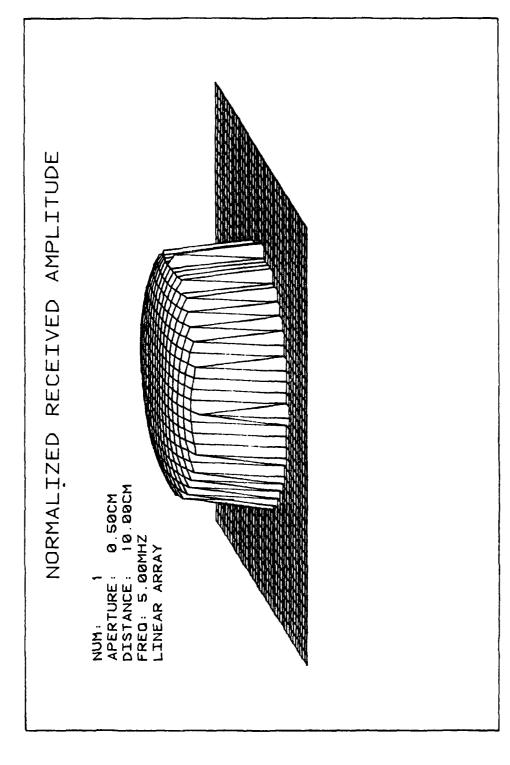
Figure 3. Phase-cancellation at the transducer surfaces of different size due to a spherical wave generated by a single scatterer located at the center of the incident beam.



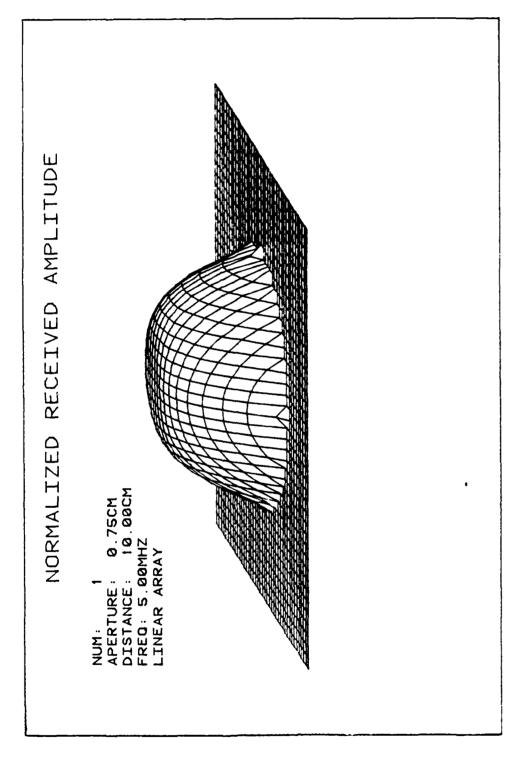
Computed normalized pressure amplitude distribution on the face of a $5.00~\rm MHz$ transducer of .10 cm in diameter situated at $10.00~\rm cm$ away from the transducer. Figure 4.



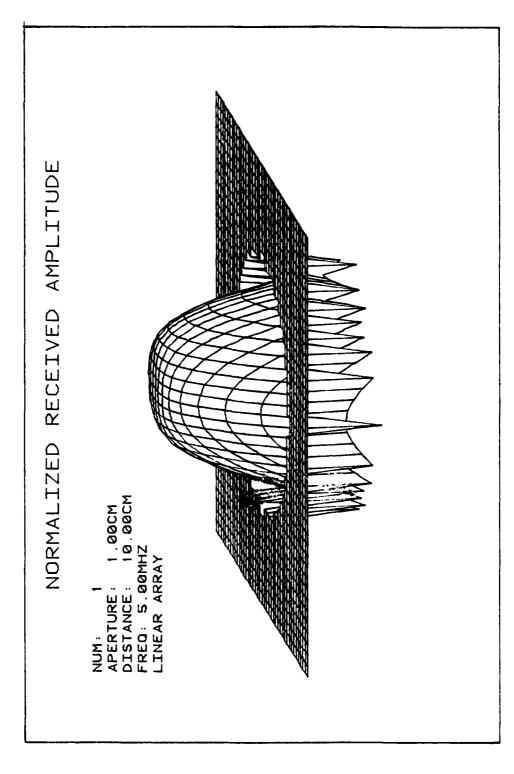
Computed normalized pressure amplitude distribution on the face of a $5.00~\mathrm{MHz}$ transducer of .25 cm in diameter situated at $10.00~\mathrm{cm}$ away from the transducer. Figure 5.



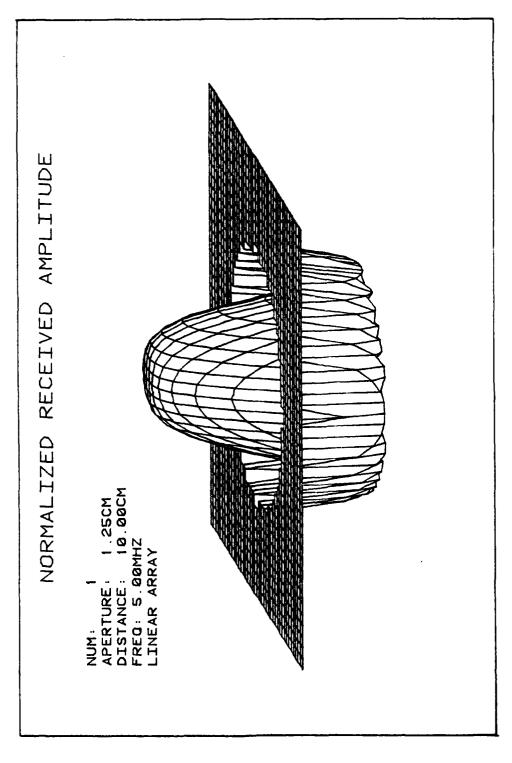
Computed normalized pressure amplitude distribution on the face of a $5.00~\mathrm{MHz}$ transducer of .50 cm in diameter situated at $10.00~\mathrm{cm}$ away from the transducer. Figure 6.



Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .75 cm in diameter situated at 10.00 cm away from the transducer. Figure 7.



Computed normalized pressure amplitude distribution on the face of a $5.00~\mathrm{MHz}$ transducer of $1.00~\mathrm{cm}$ in diameter situated at $10.00~\mathrm{cm}$ away from the transducer. Figure 8.



Computed normalized pressure amplitude distribution on the face of a $5.00~\mathrm{MHz}$ transducer of $1.25~\mathrm{cm}$ in diameter situated at $10.00~\mathrm{cm}$ away from the transducer. Figure 9.

part of the reason that 1.00 mm aperture probe has been adopted as the reference to which results obtained for transducers of larger size are compared. Results for an aperture of .25 cm, shown in Figure 5, also indicate an excellent response with little error due to phase cancellation. Upon increasing the aperture to .50 cm a slight distortion appears at the edges of the transducer resulting in a moderate 6.88% drop in the average received pressure (Figure 6). The maximum phase difference of 37.49° occurs near the edge of the transducer. The average received pressure drops an overall 31.94% as the transducer aperture is increased to .75 cm. The two-dimensional display of the phase distribution across this transducer face is shown in Figure 10. The phase value at the center of the transducer is zero degrees as discussed in the section on the mathematical formulation. To simplify the illustration without loss of meaningful data, only the integer values at each location were printed. Note the symmetry of the phase distribution across the transducer face. It follows that the amplitude distribution would also be symmetrical as seen in Figure 11. Further enlargement of the transducer apertures increases the influence of phase cancellation on the amplitude and phase distributions, average received pressure, and phase differences (Figures 8 and 9). Results for an aperture of 1.25 cm show that the amplitude pressure vary across the full range of 1.00 to -1.00; similarly, the phase varies from 0.00° to 360.00°. It is reasonable to predict, just based on these results, that experimental data measured from a transducer of this aperture (target range of 10.00 cm and frequency of 5.00 megahertz) would not best portray the acoustic properties of the material under investigation.

Target range has a strong effect on transducer performance as

<	1
įщ	1
<	1
0	ļ
	1
ĸ	-
S	1
~	-
×	1
۵.	- 1

000000000000000000000000000000000000000
000000000000000000000000000000000000000
000000000000000000000000000000000000000
00 00 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
00000000000000000000000000000000000000
00 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
000000000000000000000000000000000000000
00 00 00 00 00 00 00 00 00 00 00 00 00
00 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
00 28 7 8 7 8 7 8 7 8 7 8 7 8 7 8 7 8 7 8
0004848464646464646464646464646464646464
8 9 0 4 4 0 C C C C C C C C C C C C C C C C
00 0 7 5 4 5 6 7 6 7 6 7 6 7 6 0 0 0 0 0 0 0 0 0 0 0
00 00 00 00 00 00 00 00 00 00 00 00 00
00 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
000755660000000000000000000000000000000
00 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
00 01 0 00 00 00 00 00 00 00 00 00 00 00
00000000000000000000000000000000000000
00 000 00 00 00 00 00 00 00 00 00 00 00
00000000000000000000000000000000000000
8 7 7 7 8 9 7 7 7 7 9 9 9 9 9 9 9 9 9 9
0 C O O O O O O O O O O O O O O O O O O

NUMBER: I FREQUENCY; 5.00 MHZ
DISTANCE FROM TRANSDUCER TO SCATTER: 10.00 CM
TRANSDUCER APERATURE: 0.750 CM
DIFFERENCE: 84.34754

EJ .75 5.00 MHz transducer of ಡ Two-dimensional normalized phase distribution on the face of in aperture at a target range of $10.00~\rm{cm}$. Figure 10.

AMPLITUDE DATA

000000000000000000000000000000000000000	
00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00	
00.00 00	
0.00 0.00 0.00 0.00 0.15 0.15 0.16 0.16 0.10 0.00 0.00 0.00	
0.00 0.00 0.00 0.19 0.19 0.82 0.82 0.82 0.82 0.03 0.03 0.03 0.00 0.00	
00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00	
000877478874874874778000	
00.000 00.300 00.300 00.300 00.300 00.300 00.300 00.300 00.300 00.300 00.300 00.300	
0.00 0.34 0.34 0.34 0.34 0.93 0.99 0.99 0.99 0.99 0.99 0.99 0.99	
000000000000000000000000000000000000000	
000 000 000 000 000 000 000 000 000 00	
00000000000000000000000000000000000000	
00.000 00.300 00.300 00.300 00.300 00.300 00.300 00.300 00.300 00.300 00.300 00.300 00.300	
00.00 00	
00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00	
00000000000000000000000000000000000000	
0.00 0.00 0.15 0.15 0.15 0.15 0.15 0.15	
0.00 0.00 0.19 0.19 0.51 0.80 0.80 0.82 0.83 0.83 0.83 0.83 0.83 0.83 0.83 0.83	
0.00 0.00 0.00 0.00 0.00 0.00 0.00 0.0	
00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00 00.00	
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	

NUMBER: 1 FREQUENCY: 5.00 MHZ
DISTANCE FROM TRANSDUCER TO SCATTER: 10.00 CM
TRANSDUCER APERATURE: 0.750 CM
DIFFERENCE: 0.90151
AVERAGE RECEIVED PRESSURE: 0.68057

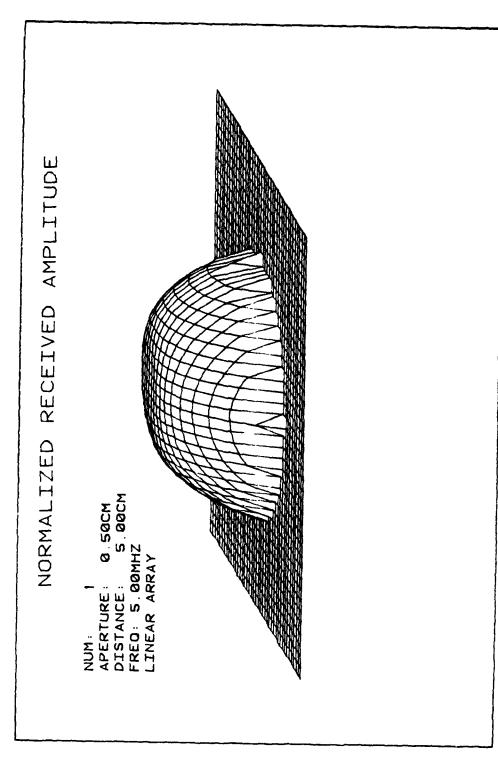
Two-dimensional normalized amplitude distribution on the face of a 5.00 MHz transducer of .75 cm in diameter at a target range of 10.00 cm. Figure 11.

well. Intuitively, as R, the distance between the transducer and scatterers is increased, the scattered wave front that reaches the receiver should more approach a plane wave due to 1/R nature of scattered spherical waves.

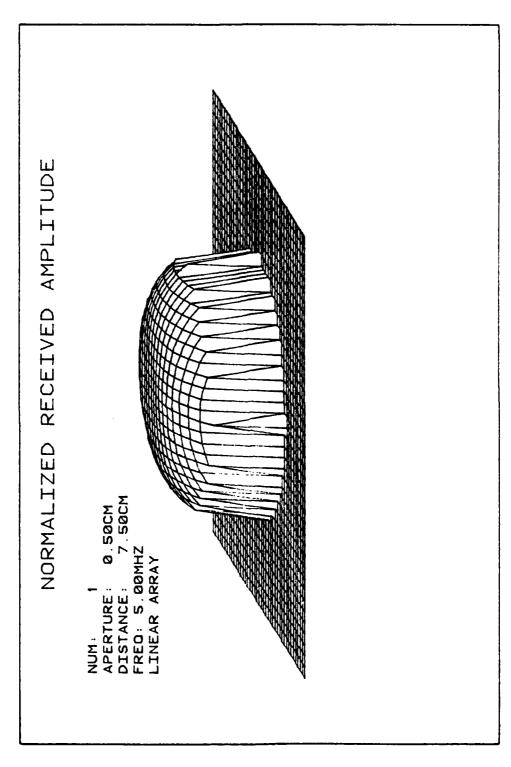
Holding aperture constant at .50 cm (frequency: 5.00 megahertz) Figures 12 through 17 demonstrate, as range is increased from 5.00 cm to 20.00 cm, the normalized received amplitude variation on the transducer face diminishes. Data also indicate, that the maximum phase differences decrease markedly from 74.95° to 18.75° for the previously mentioned range values. Distances greater than 10.00 cm indicate an error in the amplitude distribution of under 5%, which can be visually substantiated from Figure 15 through 17 where little edge distortion is evident.

A summary of average received pressure versus target range at apertures of .25, .50, .75, 1.00, 1.25, and 1.50 cm is presented in Figure 18 (frequency: 5.00 megahertz). At an aperture of 1.00 cm, minimum target ranges of 48.00 and 34.00 cm are necessary for maintaining the decreases in average received pressure at 5% and 10% respectively while ranges of only 12.00 and 9.00 cm are required for an aperture of .50 cm. Overall, this plot indicates that for apertures above .75 cm, large distances are required to reduce the phase cancellation effect.

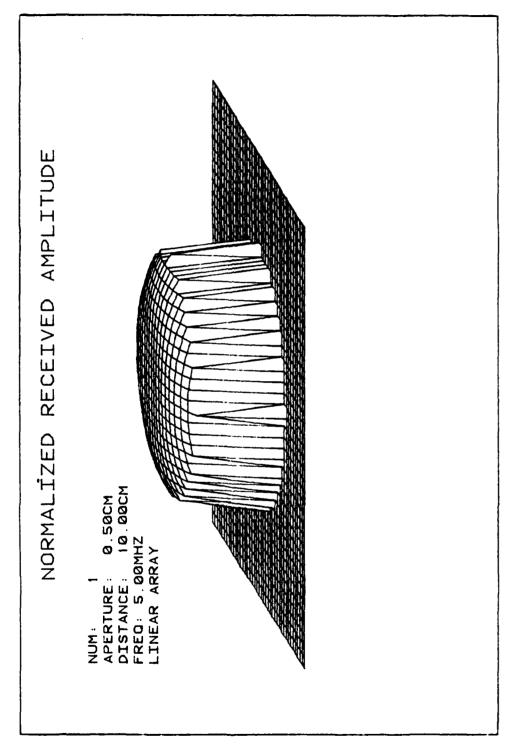
The influence of frequency on transducer performance is illustrated in Figure 19, in which average received pressure determined by transducers of various aperture sizes due to a scatterer located at 20.00 cm from the transducer is plotted versus the frequency of the wave. Clearly indicated in this figure is that phase cancellation



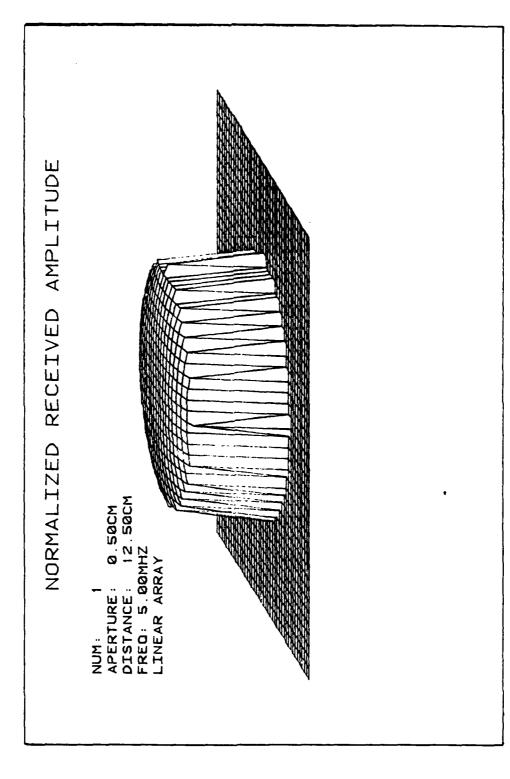
Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .50 cm in diameter at a target range of 5.00 cm. Figure 12.



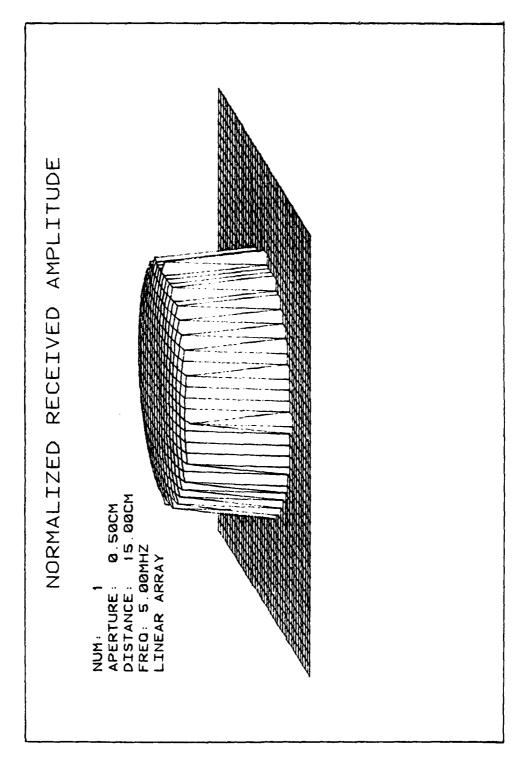
Computed normalized pressure amplitude distribution on the face of a $5.00~\rm MHz$ transducer of .50 cm in diameter at a target range of $7.50~\rm cm$. Figure 13.



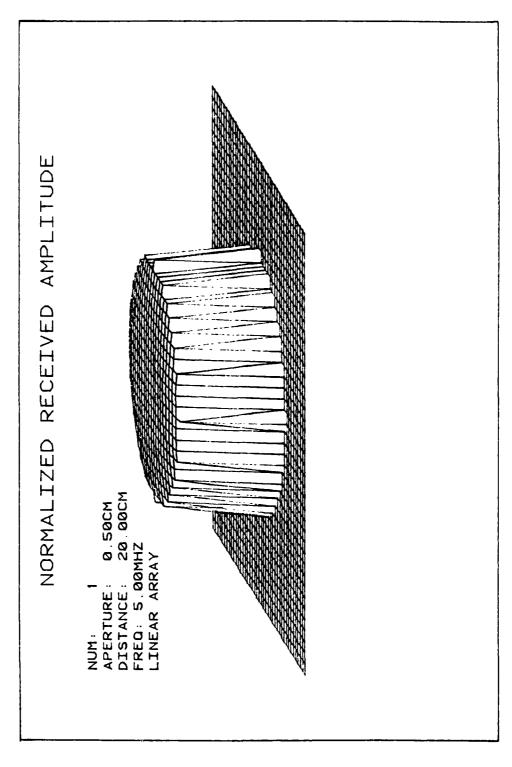
Computed normalized pressure amplitude distribution on the face of a $5.00~\mathrm{MHz}$ transducer of .50 cm in diameter at a target range of $10.00~\mathrm{cm}$. Figure 14.



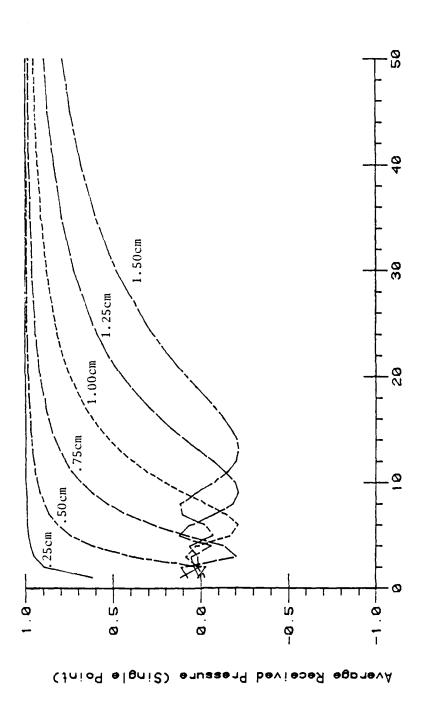
Computed normalized pressure amplitude distribution on the face of a $5.00~\rm MHz$ transducer of .50 cm in diameter at a target range of $12.50~\rm cm$. Figure 15.



Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of .50 cm in diameter at a target range of 15.00 cm. Figure 16.

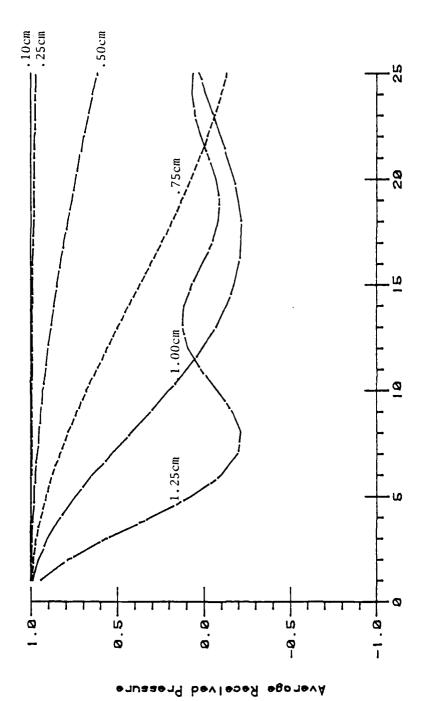


Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of ..50 cm in diameter at a target range of 20.00 cm. Figure 17.



Average received pressure measured by transducers of .25, .50, .75, 1.00, 1.25, and $1.50\,\mathrm{cm}$ in diameter due to a scatterer is plotted versus the range of the system at $5.00\,\mathrm{MHz}$. Figure 18.

Range (cm)



Frequency (megahertz)

Average received pressure measured by transducers of .10, .25, .50, .75, 1.00, and 1.25 cm in diameter due to a scutterer located 20.00 cm away is plotted versus frequency of the wave. Figure 19.

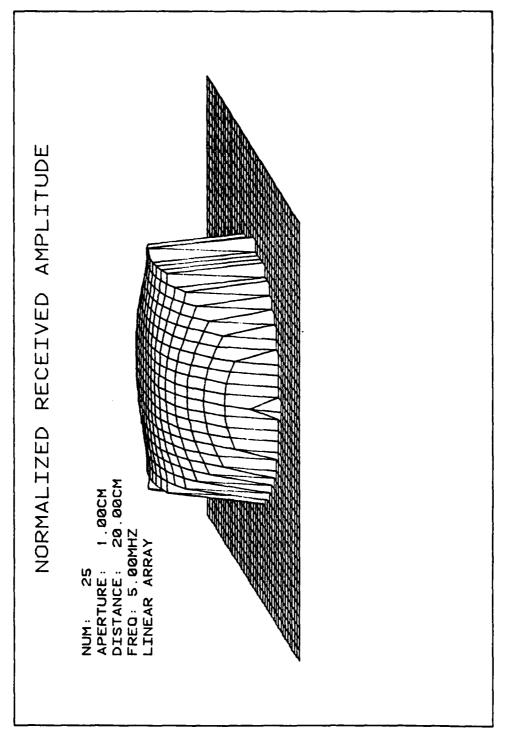
error can be reduced by using small aperture transducers and that this is especially critical for frequencies above 10.00 megahertz. Transducers with apertures less than .50 cm at frequencies under 10.00 megahertz when operated at this range suffer a maximum drop in average received pressure of less than 20%.

The above presented data for aperture, range, and frequency demonstrate a clear interrelationship between these experimental parameters and the magnitude of error induced by the phase cancellation effect.

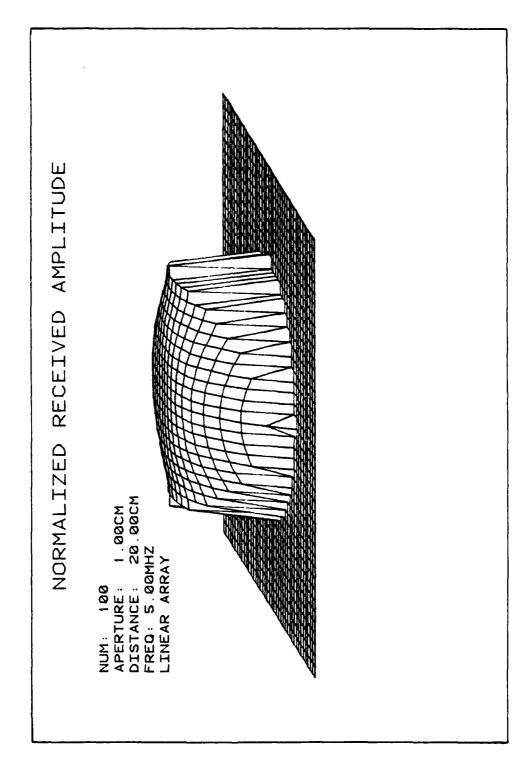
Linear Scatterer Array

The normalized pressure distribution on a 5.00 megahertz transducer surface of 1.00 cm in diameter, with 25 scatterers arranged in a linear format as indicated in Figure 2 located 20.00 cm away from the transducer, is depicted in Figure 20. This figure shows that severe destructive interference due to phase cancellation occurs near the edges of the transducer perpendicular to the axis of the array. Along these edges a maximum phase difference of 74.97° was calculated, whereas at the opposing edge, where little error is evident, a phase difference of 2.09° was determined. This amplitude distribution had an average received pressure of .8489. When the number of scatterers was increased to 100, holding all other parameters constant, only extremely small changes in the three-dimensional plot, phase difference and average received pressure occurred (less than .01%). The three-dimensional plot utilizing 100 scatterers is shown in Figure 21 and the associated average received pressure is .8485.

Further computation relating the average received pressure to the .mber of scatterers for 5.00 megahertz using different aperture



Computed normalized pressure amplitude distribution on the face of a $5.00~\mathrm{MHz}$ transducer on the face of a $5.00~\mathrm{MHz}$ transducer of $1.00~\mathrm{cm}$ in diameter due to a linear array of $25~\mathrm{scatterers}$ located $20.00~\mathrm{cm}$ away from the transducer. Figure 20.



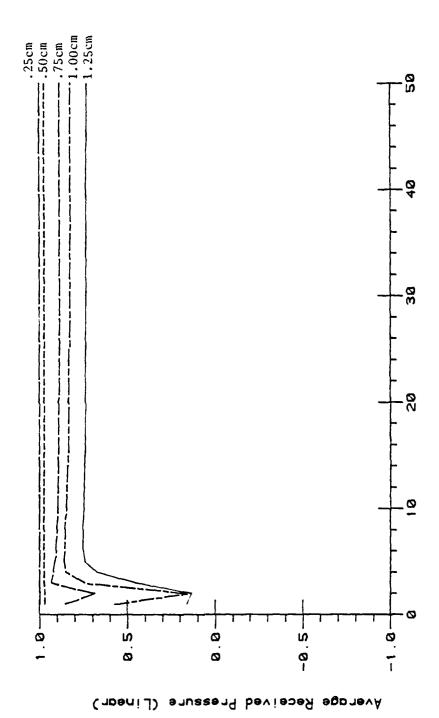
Computed normalized pressure amplitude distribution on the face of a 5.00 MHz transducer of 1.00 cm in diameter due to a linear array of 100 scatterers located 20.00 cm away from the transducer. Figure 21.

sizes at a range of 15.00 cm (Figure 22) reveals that error arising from phase cancellation is independent of the number of scatterers if that number is sufficiently large. However, this error becomes negligibly small if a small aperture is used or if the range is increased. The pronounced dip in Figure 22 at apertures of .50, .75, and 1.00 cm for two scatterers indicates the consequences of severe phase cancellation.

Rectangular and Randomly-Distributed Scatterers

These two planar enlargements have been studied most extensively even though the configuration of scatterers randomly distributed within a volume approximates more closely the real experimental arrangement in scattering measurements. This is because the computer time required for computing the results for volume scatterers is too excessive and calculations based on two-dimensional simulations may be extrapolated to the three-dimensional random volumetric distribution.

Calculations involving the rectangular and random arrays indicated that only a small number of scatterers were needed before a numeric equilibrium was reached. This conclusion supports a similar computer simulation result presented by Reid, Shung, and Kak (1979). Figure 23a summarizes results for average received pressure versus the number of scattering particles, with aperture values ranging from .25 to 1.00 cm, for a random array (range: 20.00 cm; frequency: 5.00 megahertz). For all apertures presented, a minimum of 25 scatterers were needed before oscillations damped out. This figure also provides further evidence that decreasing the aperture size increases the average received pressure seen by the receiver, and indicates apertures equal



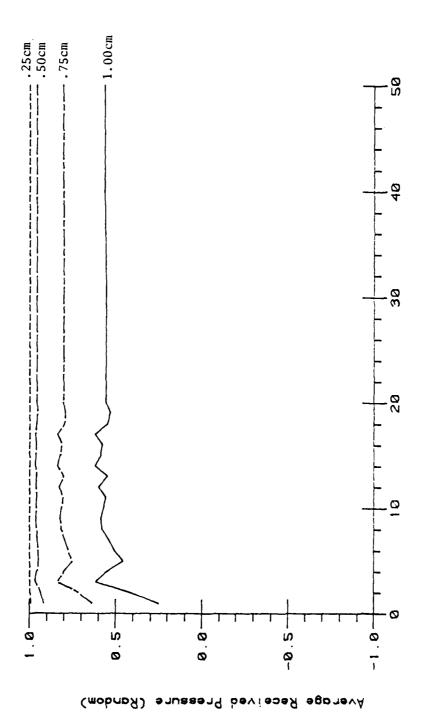
Average received pressure measured by transducers of .25, .50, .75, 1.00, and 1.25 cm in diameter at 5.00 megahertz and at a range of 20.00 cm versus the number of scatterers. Figure 22.

Number of Scatterers

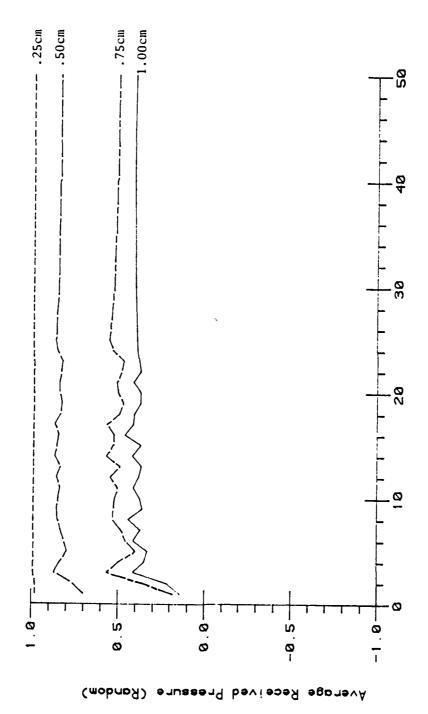
to or less than .50 cm present a signal loss of less than 10% (average received pressure greater than .9000). Figure 23b was generated utilizing identical parameters as in calculations of 23a except that the range was decreased to 10.00 cm. For an aperture of .50 cm in Figure 23a, the average received pressure was approximately .95, whereas the same aperture value in Figure 23b yielded an average received pressure of .82. Thus increasing the distance between the receiver and scatterers dramatically improves the signal strength.

In the remainder of this section, the influence of aperture on the phase cancellation effect for both the rectangular and random arrays will be further developed, and each scattering arrangement will be compared under identical parameters.

Under the more realistic conditions of the rectangular and random scattering arrangements, increasing aperture distorts the amplitude and phase distributions as shown in Figure 24, 25, and 26 for the rectangular case and Figure 27, 28, and 29 for the random case. For both cases, data were generated at a frequency of 5.00 megahertz and target range of 10.00 cm for 50 scatterers. At an aperture of .50 cm. Figures 24 and 27 demonstrate near ideal conditions for ultrasonic measurement with an overall average received pressure of .9364 and .9780 for rectangular and random distributions, respectively. An increase of aperture to .75 cm introduces a greater amount of error as shown in Figures 25 and 28. The rectangular distribution had a 16.55% drop in average received pressure while the random array distribution had a similar drop of 17.61%. The result of employing an inappropriate set of experimental conditions are illustrated in Figure 26 and 29 where severe amplitude fluctuations are seen especially in the random case.

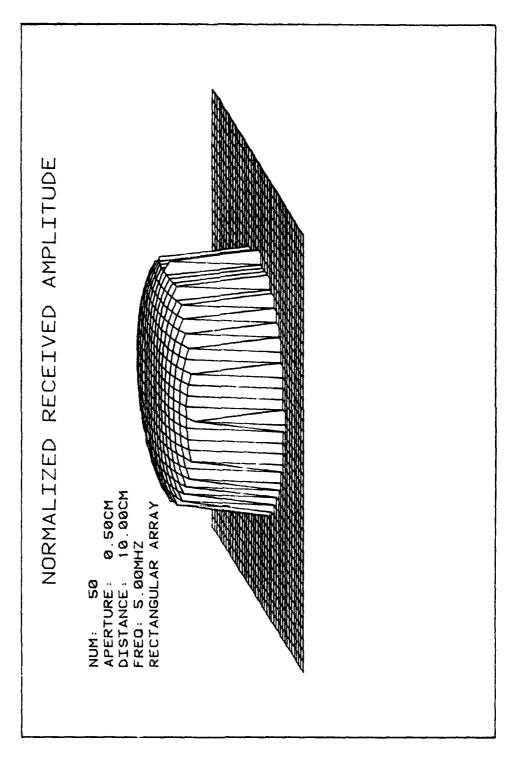


Average received pressure measured by transducers of .25, .50, .75, and 1.00 cm in diameter at 5.00 megahertz and at a range of 20.00 cm versus the number of scatterers. Number of Scatterers (Range = 20.00cm) Figure 23a,

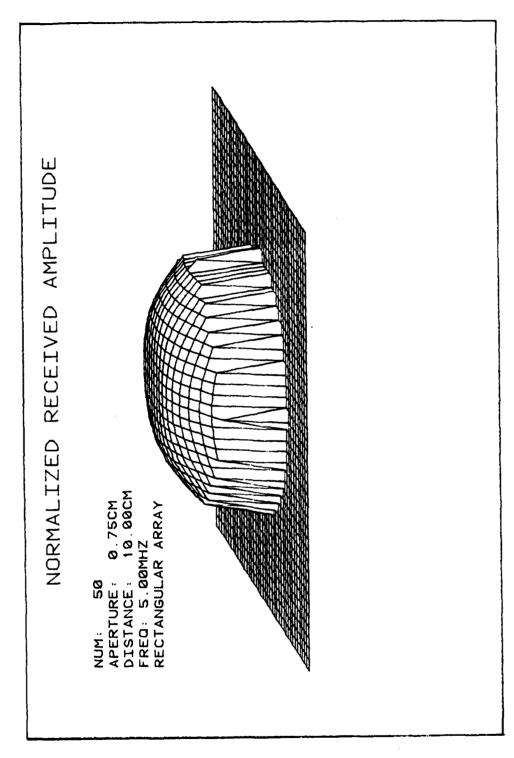


Number of Scatterers (Range = 10.00cm)

Average received pressure measured by transducers of .25, .50, .75, and 1.00 cm in diameter at 5.00 megahertz and at a range of 10.00 cm versus the number of scatterers. Figure 23b.



Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of .50 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer. Figure 24.

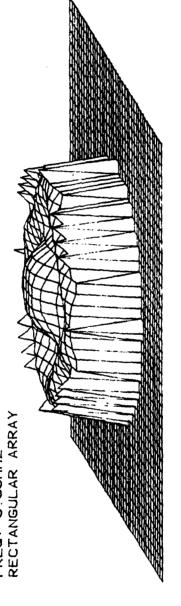


Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of .75 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer. Figure 25.

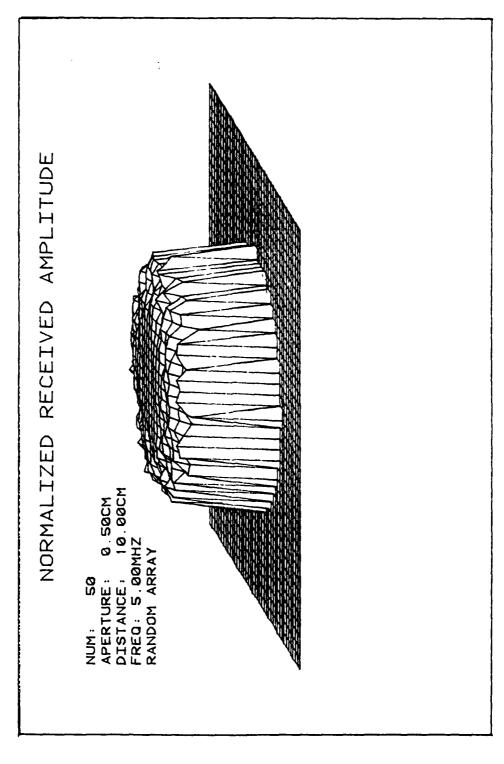
NORMALIZED RECEIVED AMPLITUDE

NUM:

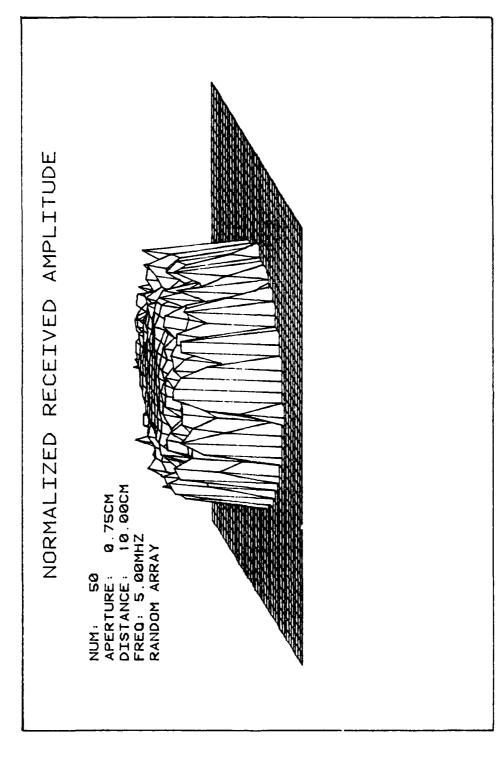
APERTURE: 1.25CM DISTANCE: 10.00CM FREO: 5.00MHZ RECTANGULAR ARRAY



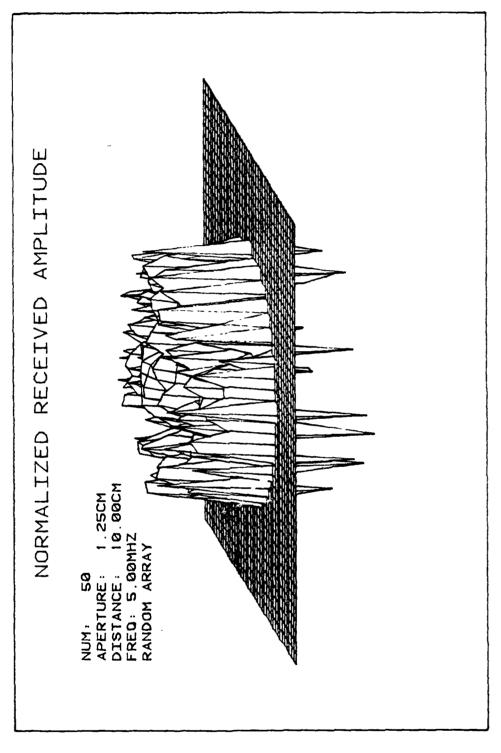
Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of 1.25 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer. Figure 26.



Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of .50 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer. Figure 27.



Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of .75 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer. Figure 28.

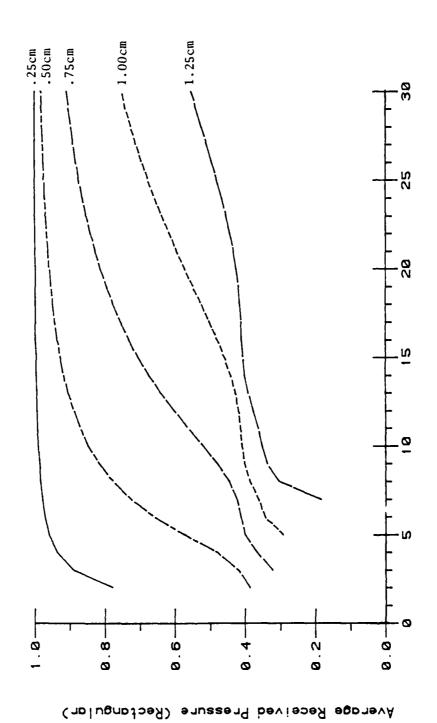


Normalized pressure amplitude distribution on the face of a 5.00 megahertz transducer of 1.25 cm in diameter due to 50 scatterers located 10.00 cm away from the transducer. Figure 29.

The average received pressure of each distribution decreased substantially (rectangular: .7708; random planar: .5255). Up to an aperture value of 1.25 cm, the results obtained for the rectangular and random planar distribution were nearly identical.

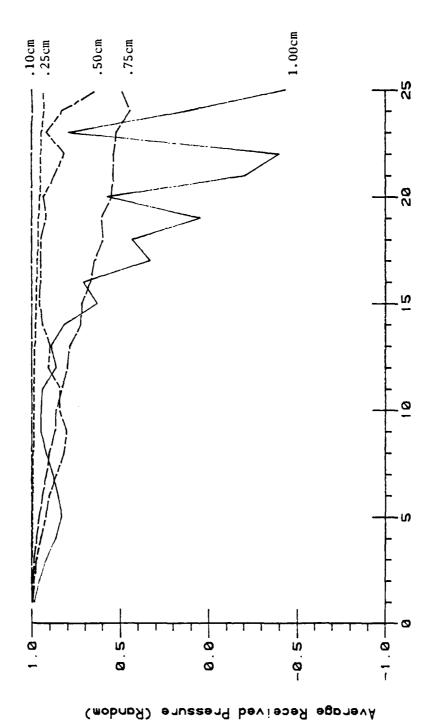
Increasing the distance between the transducer and target improves average received pressure. Figure 30 depicts average received pressure calculated at apertures of .25, .50, .75, 1.00, and 1.25 cm with 200 scatterers at a frequency of 5.00 megahertz utilizing the rectangular scattering arrangement. Apertures greater than .75 cm need values of range greater than 30.00 cm before average received pressure approaches .9000. An aperture of .25 cm needs only a range of 3.00 cm for a 10% signal drop; however, a .50 cm transducer requires 12.50 cm. To obtain an average received pressure of approximately .95, range values of 5.00 and 20.00 cm are necessary (apertures of .25 and .50 cm respectively).

Increasing frequency has a pronounced effect on errors produced by phase cancellation. This influence of frequency on average received pressure is shown by Figure 31. The average received pressure was calculated from a random distribution of 200 particles at a target range of 20.00 cm, by varying frequency at apertures of .10, .25, .50, .75, and 1.00 cm. For a frequency range of 1.00 to 10.00 megahertz, apertures of .10, .25, and .50 cm provide reasonable performance in terms of minimal signal loss due to phase cancellation. The data calculated for .10 cm transducer aperture further verifies the near ideal performance expected for a microprobe used as a receiver and its role in comparing results of various transducer apertures. When using apertures greater than .25 cm at frequencies above 10.00 megahertz, the



Average received pressure measured by transducers of .25, .50, .75, 1.00, and 1.25 cm due to 200 scatterers arranged in a rectangular distribution at 5.00 megahertz versus range. Figure 30.

Range (cm)



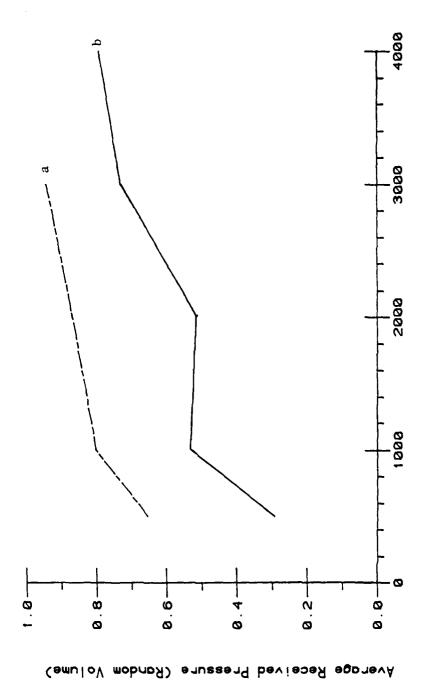
Frequency (Megahertz)

Average received pressure measured by transducers of .10, .25, .50, .75, and 1.00 cm in diameter due to 200 scatterers at a range of 20.00 cm versus frequency. Figure 31.

average received pressure declined rapidly in magnitude. See Appendix A for discussion of the oscillations.

Random Volumetric Distribution

The random volumetric scattering arrangement (illustrated in Figure 1) was simulated by a cylinder, with the base aligned parallel to the transducer face. During the simulation the diameter of the cylinder was assigned the value of the interrogating transducer aperture for simplification of geometry. Simulation results depicted by Curve a in Figure 32 for L equal to 1.00 mm, range equal to 15.00 cm, frequency equal to 5.00 megahertz and an aperture of .25 cm, demonstrated that 2500 scatterers, which correspond to a scatterer volume concentration of approximately 500 per cubic millimeter, were necessary before an average received pressure of .9 was achieved. The identical computation was performed for a cylinder depth of 2.00 mm (Curve b in Figure 32). A depth value of 1.00 mm resulted in a more rapid convergence to a low signal loss condition than a depth of 2.00 mm. It became apparent that a greater number of particles is required to obtain the same accuracy even for cases of extended range and small aperture. However, this requirement should not be of much concern in biomedical ultrasound because it is generally satisfied by biological specimens. For example, erythrocyte concentration in normal blood approaches five million per cubic millimeters.



Average received pressure measured by a .25 cm transducer at a range of 15.00 cm with a frequency of 5.00 megahertz versus the number of scatterers (Curve a: L=1.00 mm and Curve b: L=2.00 mm). Number of Scatterers Figure 32.

SUMMARY AND CONCLUSIONS

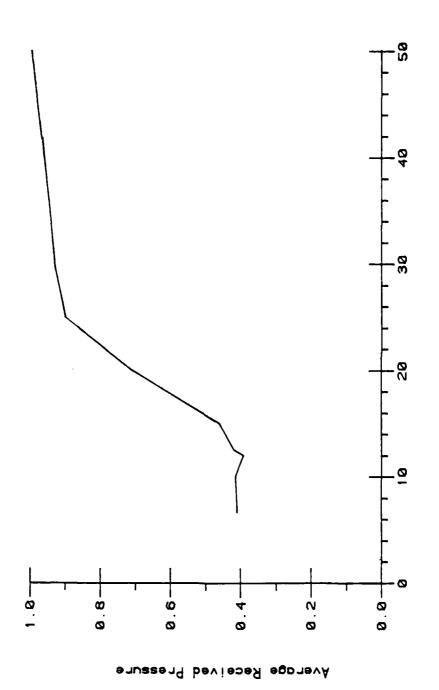
Piezoelectric transducers are sensitive to the phase of the incident pressure. Substantial error may result if such a phase-sensitive transducer is used when measuring the acoustic properties, such as attenuation and scattering, of inhomogeneous materials which distort the shape of the wave front. This is due to the phase cancellation effect. A mathematical model for the interpretation of error arising from the phase cancellation effect on the measurement of backscattered waves has been developed. A computer program was implemented on a DEC-10 to simulate the ultrasonic wave interaction between a piezoelectric transducer and an acoustic scattering environment. The influence of the phase cancellation effect on amplitude and phase distributions across the surface area of the ultrasonic receiver were quantified in terms of aperture size, frequency, target range, and number of scatterers. This investigation included varied scattering arrangements: a single point scatterer; linear, rectangular, and random arrays; and random volumetric distribution.

To minimize the influence of phase cancellation on ultrasonic measurements, proper experimental parameters such as aperture, frequency, and range may be judiciously selected. The results from this investigation are summarized in Figures 33, 34, and 35 where average received pressure is plotted versus ratios of R/D, R/F, and R λ /D (λ is wavelength, R is the range, and F is frequency) in terms of data obtained for the random array case. Although R/D and R/F are ulti-

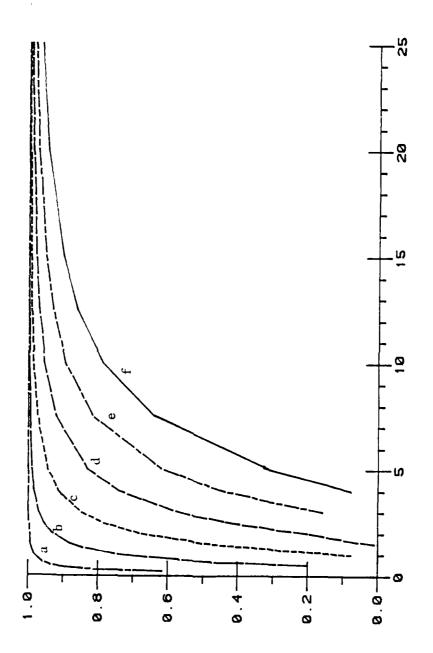
mately included within the plot of average received pressure versus $R\lambda/D$, they are useful if the researcher is constrained to a particular frequency or aperture in the experimental apparatus.

Results shown in Figure 33 indicate the necessity of high R/D values for minimization of error due to phase cancellation. These results are tabulated from data generated at 5.00 megahertz. For other frequencies, separate R/D values must be calculated. R/D values of 40.00 and 25.00 are required for 10% and 5% drops in average received pressure, respectively. The units of range and transducer diameter are centimeters.

Figure 34 represents a graphical summary of average received pressure versus R/F for apertures of .25, .50, .75, 1.00, 1.25, and 1.50 cm with the line demarking an aperture of .25 labelled a and continuing through f for each respective aperture value. R, the target range, is measured in centimeters and F is in megahertz; therefore, the units of R/F are cm-sec/cycle. Assuming a 10% drop in average received pressure (.9000) and choosing a diameter, the reader can extrapolate to the x-axis to determine the minimum R/F value. For example, selecting a diameter of 1.00 cm, a R/F of no less than 7.00 is required. For a larger diameter, a greater R/F ratio is necessary to maintain an adequate average received pressure. Furthermore, if the experiment can only tolerate a five percent drop in average received pressure (.9500), then much higher values of R/F are needed. It is important to note that for the range of frequencies most often encountered in medical imaging (1.00 to 15.00 megahertz), R/F values greater than 15.00 are desirable assuming a 10% pressure drop.



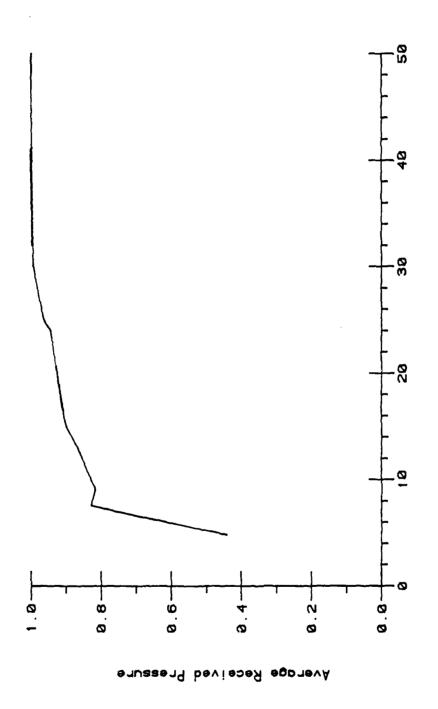
Average received pressure versus R/D for the random planar distribution. Range/Diameter Figure 33.



Average Received Pressure

Range/Frequency

Average received pressure measured by transducers of .25 (a), .50 (b), .75 (c), 1.00 (d), 1.25 (e), and 1.50 cm (f) in diameter versus R/F for the random planar distribution. Figure 34.



Average received pressure versus $R\lambda/D$ for the random planar distribution. Figure 35.

(Range * Wavelength)/Diameter

The influence of aperture, range, and frequency on the phase cancellation effect is graphically summarized in Figure 35 in which range was measured in centimeters, transducer diameter in centimeters and wavelength in millimeters. Minimum R λ /D values of 25.00 and 15.00 are necessary to achieve an experimental accuracy of 5% and 10% respectively. The units of R λ /D is in millimeters.

In conclusion, the body of data provided in this thesis should be very useful to establishing criteria which enable investigators engaged in research involving the measurements of acoustic parameters, such as attenuation and scattering of heterogeneous materials, to choose suitable experimental conditions for their measurements when phase-sensitive devices are employed.

REFERENCES

- Busse, L. J., J. G. Miller, D. E. Yuhas, J. W. Mimbs, A. N. Weiss, and B. E. Sobel. Phase Cancell lion Effects: A Source of Attenuation Artifact Eliminated by A CdS Acoustoelectric Receiver, In D. White (Ed.), <u>Ultrasound in Medicine</u> (Vol. 2). New York: Plenum Press, 1976.
- Heyman, J. S. and J. H. Cantrell, Jr. Application of An Ultrasonic

 Phase Insentive Receiver to Material Measurements, <u>IEEE Ultrasonics</u>

 Symposium Proceedings, 1977, 124-128.
- Heyman, J.S., J. H. Cantrell, Jr., and W. P. Winfree. Influence of

 Phase Cancellation and Pulse Shape Artifacts on Ultrasonic Spectrum

 Analysis, IEEE Ultrasonics Symposium Proceedings, 1979, 289-296.
- Marcus, P. W. and E. L. Carstensen. Problems with Absorption Measurements of Inhomogeneous Solids, <u>J. Acoust. Soc. Am.</u>, 1975, <u>58</u>, 1334-1335.
- Reid, J. M., K. K. Shung, and A. C. Kak. Phase-Cancellation Effects
 with Scattered Waves. <u>Proceedings of the 4th International Symposium</u>
 on Ultrasonic Imaging and Tissue Characterization, 1979, 84.

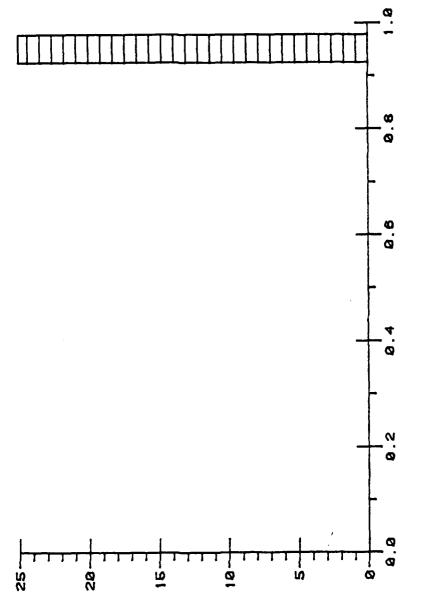
APPENDIX A

HISTOGRAM OF AVERAGE RECEIVED PRESSURE

Investigation into the variability over a series of trials of average received pressure calculated from a single point scatterer randomly placed on a plane parallel to the transducer face provides further evidence of the influence of increased aperture on the phase cancellation effect. The data was calculated by the FORTRAN program ARPVAR. Results were plotted as a histogram for each modelling condition.

For 25 trials, the average received pressure was calculated on transducer apertures of .50, .75, 1.00, and 1.25 cm (Figures 36, 37, 38, and 39) at a range of 7.50 cm and a frequency of 5.00 megahertz. For an aperture of .50 cm received pressures for all 25 trials fell within the .90 to 1.00 interval. The mean average received pressure was .9798 and had a variance of .0006. Increasing the aperture to .75 cm resulted in a decrease of the mean average received pressure to .9008 and increased sample variance to .00138. Referring to Figure 38, the variability of average received pressure outcomes increased with increasing aperture. For 1.00 cm aperture, the sample distribution had a mean of .7148 and variance of .00961. Concluding with Figure 39, an aperture of 1.25 cm shows the large fluctuations in average received pressure due to phase cancellation calculated for a single point scatterer. This outcome is expected and emphasizes that correct aperture size is extremely important when utilizing phasesensitive piezoelectric transducers.

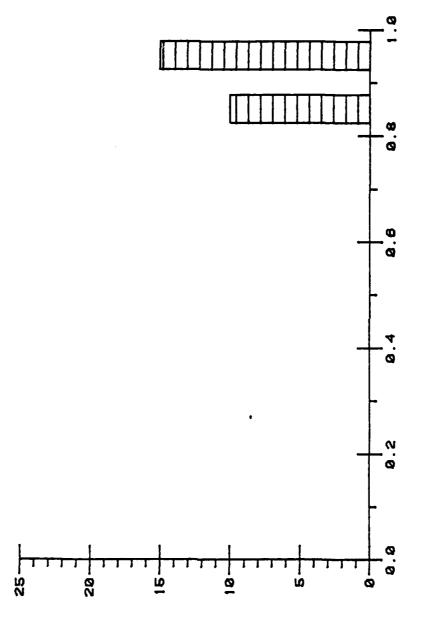
The variability of average received pressure was investigated at a range of 20.00 cm, a frequency of 25.00 megahertz and 200 scatterers for apertures of .50, .75, and 1.00 cm (Figures 40, 41, and 42). Twenty-five trials were performed at each of these aperture values. These parameters were chosen in order to compare data summarized in Figure 31. In Figure 31, each point was obtained from only one trial. As evident from Figures 41 and 42, there is considerable variation from trial to trial for apertures of .75 and 1.00 cm and results of one trial are not representative of the typical outcome under these conditions. For example, the results in Figure 42 demonstrate a large variance in average received pressure when using a 1.00 cm aperture transducer. The sample mean of this distribution is .2525 and has a variance of .0463. The consequence is that results obtained from one trial may differ substantially from the other. Therefore, data for higher frequencies, e.g., data above 13.00 megahertz at an aperture of 1.00 cm and above 22.00 megahertz at an aperture of .75 cm would be expected to show considerable variation for different arrangements of 200 scatterers. This result explains the large fluctuations seen in Figure 31 at higher frequencies for large apertures.



Mumber of Occurences

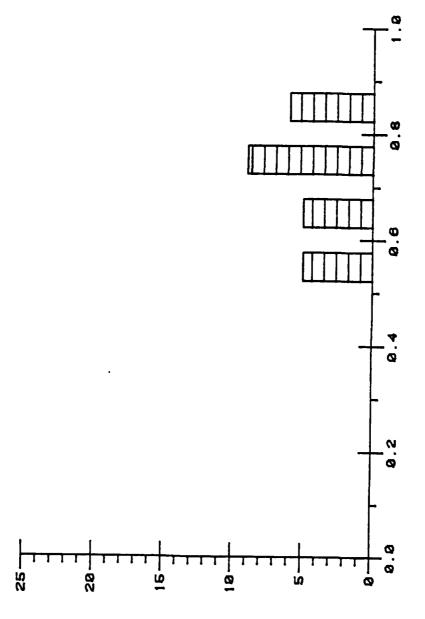
Average Received Pressure

Average received pressure versus the number of occurrences for a single point scatterer at a range of 7.50 cm and aperture of .50 cm over 25 trials. Figure 36.



Number of Decurences

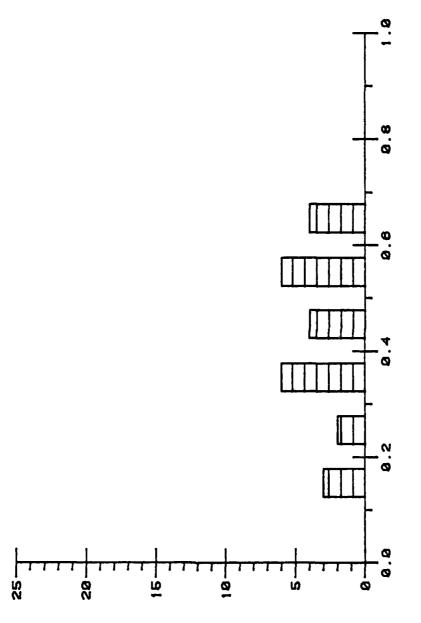
Average received pressure versus the number of occurrences for a single point scatterer at a range of 7.50 cm and aperture of .75 cm over 25 trials. Average Received Pressure Figure 37.



Number of Occurences

Average Received Pressure

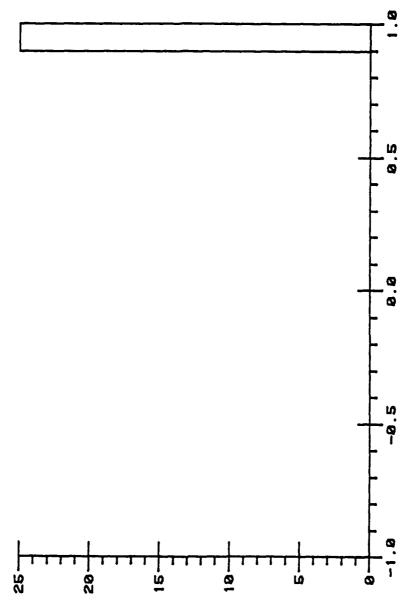
Average received pressure versus the number of occurrences for a single point scatterer at a range of 7.50 cm and aperture of 1.00 cm over 25 trials. Figure 38.



Mumber of Occurences

Average Received Pressure

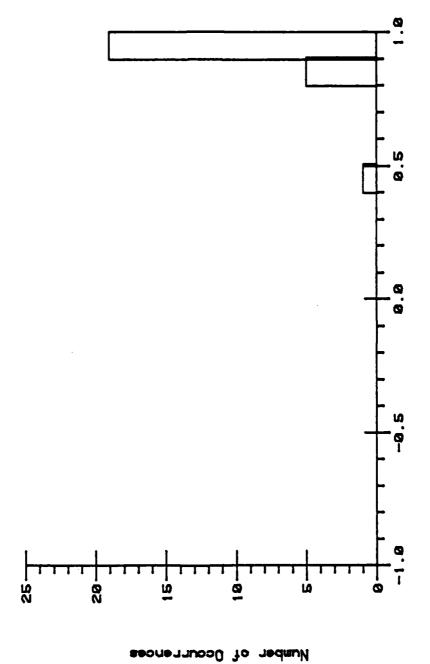
Average received pressure versus the number of occurrences for a single point scatterer at a range ${\rm c}^{\it f}$ 7.50 cm and aperture of 1.25 cm over 25 trials. Figure 39.



Number of Occurrences

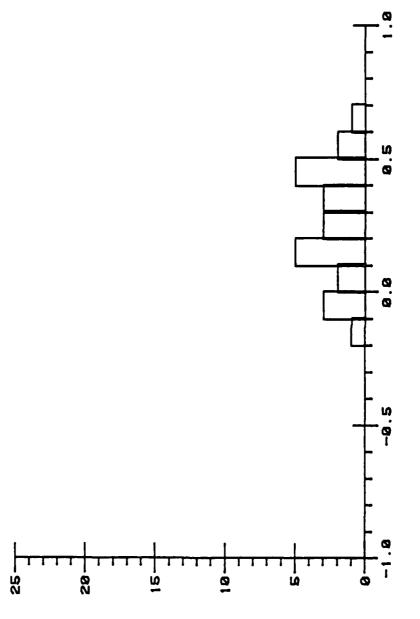
Average Received Pressure

Average received pressure versus the number of occurrences for 200 scatterers at a range of 20.00 cm and aperture of .50 cm over 25 trials. Figure 40.



Average Received Pressure

Average received pressure versus the number of occurrences for 200 scatterers at a range of 20.00 cm and aperture of .75 cm over 25 trials. Figure 41.



Number of Occurrences

Average Received Pressure

Average received pressure versus the number of occurrences for 200 scatterers at a range of 20.00 cm and aperture of 1.00 cm over 25 trials. Figure 42.

APPENDIX B

HOW TO USE THE COMPUTER PROGRAMS

The computer programs used in this simulation were written to allow maximum flexibility and accurate presentation of data generated in the modelling procedure. The author made extensive use of modular program construction so that other workers can clearly understand program execution and implement source code modification. The operating requirements and logic flow of each computer program are presented.

Phase

A FORTRAN program PHASE was developed for use in the computer simulation. This program allows the user to select the following scattering arrangements: a single point source, linear array, rectangular array, random planar array, and random volume. The user also specifies aperture, number of scatterers, range and frequency for calculations of received amplitude and phase distributions across the surface area of the ultrasonic transducer. Once the program PHASE has been loaded, the program will prompt the user for input parameters as shown by Figure 43. Initial calculations are displayed on the computer terminal for verification by the user. The resulting data calculated can be printed on paper and/or written to a disk file for plotting by PLT3D, CPLOT, or other available x-y plotting routines.

PHASE-CANCELLATION PROGRAM

SCATTERER ARRANGEMENT(L, 0, R, V, A):

SPECIFY NUMBER OF SCATTERING PARTICLES:

ENTER DISTANCE FROM TRANSDUCER TO PARTICLES:

TRANSDUCER APERTURE:

PLEASE ENTER OPERATING FREQUENCY (MEGAHERTZ):

VARY RANGE, SCATTERERS, APERTURE, FREQUENCY(R, U, A, F):

ENTER STOP VALUE(REAL):

INCREMENT:

DO YOU WANT PLOTTING DATA WRITTEN TO DISK(Y/N):

PRINTED DATA WRITTEN TO DISK(Y/N):

IS ABOVE INPUT DATA CORRECT(Y/N):

Figure 43. Sample input to program PHASE.

```
Bioengineering: Phase-Cancellation Studies
C
   SCATTERERING ARRANGEMENTS:
      1) LINEAR
C
      2) RECTANGULAR ARRAY
C
      RANDOM ARRAY
      4) RANDOM VOLUME
      5) RANDOM ARRAY CONSTANT SCATTERING APERTURE
C**********************
        COMPLEX PRS(41,41)
        COMMON /B/RANGE, NUM, APERT, FREQ, WAVEL, XK, PARRAD, NCOUNT, PCT, PSF,
        1 DIV, XNEAR, IFLAG, IFLAG1, IFLAG2, IFLAG3, VELCTY, XKA, RFREQ(100),
        2 TRANR, AMP(41,41), THETA(41,41), ASF, RPHASE(100), RREAL(100),
        3 SCAT, CENTER, M, AMPMIN, AMPMAX, THEMIN, THEMAX, PIC(41,41), DIM,
        4 RNUM(100), RPRS(100), RMAG(100), RIMAG(100), DAMP, DTHETA, RPCT(100),
        5 TEMPRS, ANS, RAMP(100), STOP, XINC, SCTANS, XNUM, RVOL(100), ARPVOL, PRS
C
                               MAIN PROGRAM
        TYPE 1000
1000
        FORMAT(26X, 'BIOENGINEERING PROGRAM', //)
        CALL ASK
 1005
        CALL INIT
        CALL CRUNCH
        CALL WARN
        CALL ARYPIC
        CALL DECIDE
        CALL VERIFY
        CALL NORMAL
        CALL STAT
        CALL AVGPRS
        CALL FILINC
        CALL INCVAR
        IF(IFLAG2.EQ.O) GOTO 1005
2050
        TYPE 2055
2055
        FORMAT('ODO YOU WISH TO CONTINUE(Y/N)? ',$)
        CALL BELL
        ACCEPT 2060, ANSWER
2060
        FORMAT(A1)
        IF(ANSWER.NE.'Y') GOTO 2070
        CALL ASK
        GOTO 1005
2070
        CALL PARCNT
        CALL SAVDAT
        CALL VOLDAT
        STOP
        END
```

```
C*********************
 PRIDAT: PRINT RESULTS OF AMPLITUDE AND PHASE CALCULATIONS
        SUBROUTINE PRTDAT(FNAME3, FNAME4)
        DOUBLE PRECISION FNAME3, FNAME4
        INTEGER ITHETA(41,41)
        CALL OPEN(21, 'FILE', FNAME3)
        CALL OPEN(22, 'FILE', FNAME4)
        WRITE(21,2076)
        FORMAT(53x, 'AMPLITUDE DATA')
2076
        WRITE(22,2077)
 2077
        FORMAT(58X, 'PHASE DATA')
        WRITE(21,2078)
 2078
        FORMAT(53x,14('-'),//)
        WRITE(22,2079)
2079
       FORMAT(58x, 10('-'), //)
        DO 2090 I = 1.M
        DO 2091 J = 1, M
 2091
        ITHETA(I,J) = INT(THETA(I,J))
 2090
        CONTINUE
        WRITE(21,2085)((AMP(I,J),J=9,33),I=9,33)
        WRITE(22,2086)((ITHETA(I,J),J=9,33),I=9,33)
2085
        FORMAT(25(F5.2))
2086
       FORMAT(25(I4,1X))
        WRITE(21,2081)
        WRITE(22,2081)
                  ′,///)
2081
        FORMAT('
        IF(SCTANS.EQ.'O') WRITE(21,2093) PCT, FREQ
        IF(SCTANS.EQ.'O') GOTO 2094
 2093
        FORMAT(1X, 'NUMBER:', F8.1,7X, 'FREQUENCY:', F5.2, 'MHZ')
        WRITE(21,2082) NUM, FREQ
        WRITE(22,2082) NUM, FREQ
        FORMAT(1X,'NUMBER:',15,10X,'FREQUENCY:',F5.2,' MHZ')
 2082
 2094
        WRITE(21,2083) RANGE
        WRITE(22,2083) RANGE
 2083
        FORMAT(1X, 'DISTANCE FROM TRANSDUCER TO SCATTER:', F7.2, 'CM')
        WRITE(21,2084) APERT
        WRITE(22,2084) APERT
        FORMAT(1X, 'TRANSDUCER APERATURE:', F6.3,' CM')
 2084
        WRITE(21,2088) DAMP
        WRITE(22,2088) DTHETA
        FORMAT(1X,'DIFFERENCE:',F11.5)
 2088
        WRITE(21,2092) TEMPRS
 2092
        FORMAT(1X, 'AVERAGE RECEIVED PRESSURE:',F10.5)
        CALL CLOSE(21)
        CALL CLOSE(22)
        RETURN
        END
```

```
C**************
  PRTDAT: PRINT RESULTS OF AMPLITUDE AND PHASE CALCULATIONS
C**********************
        SUBROUTINE PRTDAT(FNAME3, FNAME4)
        DOUBLE PRECISION FNAME3, FNAME4
        INTEGER ITHETA(41,41)
        CALL OPEN(21, 'FILE', FNAME3)
CALL OPEN(22, 'FILE', FNAME4)
        WRITE(21,2076)
 2076
        FORMAT(53X, 'AMPLITUDE DATA')
       WRITE(22,2077)
2077
        FORMAT(58X, 'PHASE DATA')
        WRITE(21,2078)
2078
        FORMAT(53X, 14('-'),//)
       WRITE(22,2079)
2079
        FORMAT(58X, 10('-'), //)
        DO 2090 I = 1, M
        DO 2091 J = 1, M
 2091
        ITHETA(I,J) = INT(THETA(I,J))
 2090
        CONTINUE
        WRITE(21,2085)((AMP(I,J),J=9,33),I=9,33)
        WRITE(22,2086)((ITHETA(I,J),J=9,33),I=9,33)
2085
        FORMAT(25(F5.2))
2086
        FORMAT(25(14,1X))
       WRITE(21,2081)
        WRITE(22,2081)
        FORMAT('
 2081
                   ′,///)
        IF(SCTANS.EQ.'O') WRITE(21,2093) PCT, FREQ
        IF(SCTANS.EQ.'O') GOTO 2094
        FORMAT(1X, 'NUMBER: ', F8.1, 7X, 'FREQUENCY: ', F5.2, 'MHZ')
 2093
        WRITE(21,2082) NUM, FREQ
        WRITE(22,2082) NUM, FREQ
 2082
        FORMAT(1X, 'NUMBER:', 15, 10X, 'FREQUENCY:', F5.2, 'MHZ')
2094
        WRITE(21,2083) RANGE
        WRITE(22,2083) RANGE
 2083
        FORMAT(1X, 'DISTANCE FROM TRANSDUCER TO SCATTER:', F7.2)
        WRITE(21,2084) APERT
        WRITE(22,2084) APERT
 2084
        FORMAT(1X, 'TRANSDUCER APERATURE: ', F6.3, 'CM')
        WRITE(21,2088) DAMP
        WRITE(22,2088) DTHETA
 2088
        FORMAT(1X, 'DIFFERENCE:', F11.5)
       WRITE(21,2092) TEMPRS
 2092
        FORMAT(1X, 'AVERAGE RECEIVED PRESSURE:',F10.5)
        CALL CLOSE(21)
        CALL CLOSE(22)
        RETURN
        END
```

```
C*********************
  AVGPRS: CALCULATE AVERAGE RECEIVED PRESSURE FOR THE TRANSDUCER
SUBROUTINE AVGPRS
      K = 0
      TEMPRS = 0.0
      DO 3005 I = 1, M
      DO 3000 J = 1.M
      IF(PIC(I,J).EQ.'-') GOTO 3000
      TEMPRS = TEMPRS + AMP(I,J)
      K = K + 1
3000
      CONTINUE
3005
      CONTINUE
      TEMPRS = TEMPRS/FLOAT(K)
      RPRS(NCOUNT) = TEMPRS
      AREA = 3.1415927 * (TRANR**2)
      APRESS = (TEMPRS/AREA)
      TYPE 3010, APRESS, TEMPRS
3010
      FORMAT('OAVGPRS/AREA = ',F11.5,' AVGPRS =',F11.5)
      IF(SCTANS.NE.'V') GOTO 3025
      VOLUME = 3.1415926 * (TRANR**2) * .1
      ARPVOL = TEMPRS/VOLUME
      RVOL(NCOUNT) = ARPVOL
3025
      RETURN
      END
C*********************************
С
С
 CRUNCH: CALCULATE SCALE FACTORS
С
C***********************************
      SUBROUTINE CRUNCH
      NNUM = NUM
      IF(NUM.EQ.1) NNUM = NNUM + 1
      XNUM = FLOAT(NNUM)
      PSF = (APERT/(XNUM-1.0))
      CENTER = INT(M/2.0) + 1.0
      TRANR = (APERT/2.0)
      ASF = (APERT/(DIM-1.00))
      PARRAD = 6.0
      RETURN
      END
```

```
INFO: WRITE INFORMATION TO DISK IN FILE INFXXX.DAT
C****************
       SUBROUTINE INFO(FNAME1, FNAME2)
       DOUBLE PRECISION FNAME1, FNAME2
       CALL OPEN(21, 'FILE', FNAME2)
       WRITE(21,4000)
4000
       FORMAT(26X, 'INFORMATION FILE')
       WRITE(21,4005)
4005
       FORMAT(26X, 16('-'), ///)
       WRITE(21,4010) FNAME1
4010
       FORMAT(5X, 'PLOTTING DATA FILE NAME: ',A10,/)
       WRITE(21,4015) NUM
       FORMAT(5X, 'NUMBER OF SCATTERING PARTICLES:',15,/)
 4015
       WRITE(21,4020) RANGE
4020
       FORMAT(5X, 'DISTANCE TRANSDUCER - SCATTERERS: ', F7.2, 1X, 'CM', /)
       WRITE(21,4025) APERT
       FORMAT(5X, 'APERATURE OF TRANSDUCER:', F8.3, 1X, 'CM', /)
4025
       WRITE(21,4035) FREQ
 4035
       FORMAT(5x,'FREQUENCY:',F7.2,1x,'MEGAHERTZ',/)
       WRITE(21,4040) WAVEL
       FORMAT(5x,'WAVELENGTH:',F7.2,1x,'MILLIMETERS',/)
4040
       WRITE(21,4045) XK
 4045
       FORMAT(5X, 'WAVENUMBER K:',F10.2,' RAD/CM',/)
       WRITE(21,4050) PARRAD
       FORMAT(5X, 'SCATTERER RADIUS:',F7.2,1X, 'MICROMETERS',/)
 4050
       WRITE(21,4060) DIV
 4060
       FORMAT(5x, 'ANGLE OF DIVERGENCE:', F7.2, 1x, 'DEGREES', /)
       WRITE(21,4065) XNEAR
       FORMAT(5X,'NEAR-FARFIELD BOUNDARY:',F7.2,1X,'CENTIMETERS',/)
 4065
       WRITE(21,4070) VELCTY
       FORMAT(5x,'WAVESPEED:',F8.2,1x,'METERS/SEC',/)
 4070
       WRITE(21,4075) XKA
 4075
       FORMAT(5X, 'KA:', F8.5, /)
       WRITE(21,4080) SCAT
 4080
       FORMAT(5X, 'SCATTERING PARTICLE COEFFICIENT:', F5.2, /)
       WRITE(21,4090) SCTANS
 4090
       FORMAT(5X, 'SCATTERERING ARRANGEMENT: ',A1,/)
       WRITE(21,4100) TEMPRS
 4100
       FORMAT(5x, 'AVERAGE RECEIVED PRESSURE =',F11.5,/)
       WRITE(21,4105) DAMP
 4105
       FORMAT(5X, 'AMPLITUDE DIFFERENCE - TRANSDUCER = ',F11.6,/)
       WRITE(21,4110) DTHETA
 4110
       FORMAT(5X, 'PHASE DIFFERENCE ACROSS TRANSUCER = ',F11.6,/)
       CALL CLOSE(21)
       RETURN
       END
```

```
VERIFY: DISPLAY INFORMATION ON TTY FOR VERIFERCATION
SUBROUTINE VERIFY
      TYPE 5000
5000
      FORMAT('0
      TYPE 5005
5005
      FORMAT(26x,'INPUT DATA SUMMARY',/)
      TYPE 5010, NCOUNT, PCT
5010
      FORMAT('ONCOUNT:', 16, 25x, 'NUMBER OF PARTICLES', F7.1)
      TYPE 5015, RANGE, APERT
5015
      FORMAT('OLENGTH FACE TO PARTICLES', F7.2, 7X, 'APERATURE: 'F8.3)
      TYPE 5020, WAVEL, XK
5020
      FORMAT('OWAVELENGTH:', F7.2, 20X, 'WAVENUMBER:', F10.2,' RAD/CM')
      TYPE 5025, PARRAD, FREQ
5025
      FORMAT('OPARTICLE RADIUS:', F7.2, 15x, 'FREQ:', F7.2, 1x, 'MHERTZ')
      TYPE 5030, DIV, XNEAR
5030
      FORMAT('ODIVERGENCE:', F7.2, 20X, 'NEARFIELD BOUNDARY:', F7.2)
      RETURN
      END
INIT: INTIALIZE ULTRASONIC AND ARRAY PARAMETERS
SUBROUTINE INIT
      M = 41
      DIM = 23.0
      SCAT = 1.0
      VELCTY = 1500.00
      WAVEL = (VELCTY/(FREO*1.0E03))
      XK = (2.0 * 3.14159)/(WAVEL/10.0)
      XNEAR = (APERT**2)/(.40 * WAVEL)
      DIV = (ASIN((.122 * WAVEL)/APERT)) * 57.29578
      NCOUNT = NCOUNT + 1
      AMPMIN = 1000.00
      AMPMAX =-1000.00
      THEMIN = 1000.00
      THEMAX =-1000.00
      RETURN
      END
```

```
C************************
  SAVDAT: CREATE DATA FILE FOR PLOTTING OF AVERAGE AMPLITUDE
  VS. NUMBER OF SCATTERERS AND WRITE DATA SUMMARY FILE TO DISK
C**********************
        SUBROUTINE SAVDAT
        DOUBLE PRECISION FNAME5, FNAME6
        CALL NAME(FNAME5, FNAME6)
        CALL OPEN(21, 'FILE', FNAME5)
        CALL OPEN(22, 'FILE', FNAME6)
       WRITE(22,8010)
8010
       FORMAT(35X, 'DATA SUMMARY')
       WRITE(22,8015)
        FORMAT(35X,12('-'),///)
8015
       WRITE(22,8016) SCTANS
8016
       FORMAT(6X, 'SCATTERERING ARRANGEMENT: ',A1,//)
        IF(ANS.NE.'F') GOTO 8022
        WRITE(22.8021) RANGE, APERT, NUM
                                       APERT:', F6.3,' CM NUM: ', 15,//)
8021
       FORMAT(6X, 'RANGE:', F7.2,' CM
       WRITE(22,8026)
       FORMAT(5x, 'FRQ', 4x, 'AVG PRS', 4x, 'DIFF AMP', 4x, 'DIFF PHASE', 4x,
8026
        1 'REAL',5X,'IMAGINARY',4X,'MAGNITUDE')
       GOTO 8002
8022
       WRITE(22,8020) RANGE, APERT, FREQ
       FORMAT(6X, 'RANGE:', F7.2,' CM
8020
                                          APERT: ', F6.3,' CM
                                                               FREQ: ',
        1 F5.2, MEGAHERTZ',//)
        WRITE(22,8025)
8025
       FORMAT(5X,'NUM',4X,'AVG PRS',4X,'DIFF AMP',4X,'DIFF PHASE',4X,
        1 'REAL', 5X, 'IMAGINARY', 4X, 'MAGNITUDE')
8002
       WRITE(22,8030)
8030
       FORMAT(5x,'---',4x,7('-'),4x,8('-'),4x,10('-'),4x,'----',5x,
        1 9('-'),4x,9('-'),//)
        DO 8000 I = 1, NCOUNT
        IF(ANS.NE.'F') GOTO 8001
        WRITE(21,8005) RFREQ(1), RPRS(1)
        WRITE(22,8040) RFREQ(I),RPRS(I),RAMP(I),RPHASE(I),RREAL(I),
        1 RIMAG(I), RMAG(I)
       GOTO 8000
8001
       WRITE(21,8005) RNUM(I), RPRS(I)
8035
        WRITE(22,8040) RNUM(I),RPRS(I),RAMP(I),RPHASE(I),RREAL(I),
        1 RIMAG(I),RMAG(I)
8005
       FORMAT(3X,F11.4,2X,F11.7)
       FORMAT(3X, F6.0, 2X, F9.5, 3X, F7.3, 7X, F7.3, 4X, F7.3, 5X, F7.3, 5X, F7.3)
8040
8000
        CONTINUE
        CALL CLOSE(21)
        CALL CLOSE(22)
        RETURN
        END
```

```
C
  ARYPIC: INTIALIZE PICTATORIAL TRANSDUCER REPRESENTATION
  ROUTINE LOCATES PARTICLE SCATTERERS WITHIN TRANSDUCER BEAM
C**********************
       SUBROUTINE ARYPIC
       DO 6005 I = 1, M
       DO 6000 J = 1, M
       PIC(I,J) = '-'
       AMP(I,J) = 0.0
6000
       THETA(I,J) = 0.0
6005
       CONTINUE
       RETURN
       END
C***********************
С
  PLTDAT: WRITE PLOTTING DATA TO DISK
C**********************
       SUBROUTINE PLTDAT(FNAME1)
       DOUBLE PRECISION FNAME1
       CALL OPEN(21, 'FILE', FNAME1)
       WRITE(21,7000) M, AMPMIN, AMPMAX, THEMIN, THEMAX, SCTANS
 7000
       FORMAT(13, 1X, F11.5, 1X, F11.5, 1X, F11.5, 1X, F11.5, 1X, A1)
       WRITE(21,7005) NUM, TRANK, RANGE, FREQ, APERT, PCT
 7005
       FORMAT(I5, 1X, F11.5, 1X, F11.5, 1X, F11.5, 1X, F11.5)
       WRITE(21,7010)((AMP(I,J),J=1,M),I=1,M)
       WRITE(21,7010)((THETA(I,J),J=L,M),I=1,M)
7010
       FORMAT(41(F11.6,1X))
       CALL CLOSE(21)
       RETURN
       END
```

· `,

```
C***********************
 ASK: PROMPT USER FOR INPUT VARIABLES
C*********************
       SUBROUTINE ASK
8000
       IFLAG = 0
       IFLAG1 = 0
8002
       TYPE 8003
8003
       FORMAT('OSCATTERER ARRANGEMENT(L,0,R,V,A): ',$)
       ACCEPT 8055, SCTANS
       TYPE 8001
8001
       FORMAT('OSPECIFY NUMBER OF SCATTERING PARTICLES: ',$)
       ACCEPT 8005, NUM
8005
       FORMAT(I)
       TYPE 8010
8010
       FORMAT('OENTER DISTANCE FROM TRANSDUCER TO PARTICLES: ',$)
       ACCEPT 8015, RANGE
8015
       FORMAT(F)
       TYPE 8020
8020
       FORMAT('OTRANSDUCER APERTURE: ',$)
       ACCEPT 8015, APERT
       TYPE 8030
8030
       FORMAT('OPLEASE ENTER OPERATING FREQUENCY(MEGAHERTZ): ',$)
       ACCEPT 8015, FREQ
8045
       TYPE 8050
       FORMAT('ORANGE, NUMBER SCATTERERS, APERTURE, FREQ(R, N, A, F): ',$)
8050
       ACCEPT 8055, ANS
8055
       FORMAT(A1)
       IF(ANS.NE.'R'.AND.ANS.NE.'N'.AND.ANS.NE.'A'.AND.ANS.NE.'F')
       1 GOTO 8045
       TYPE 8070
8070
       FORMAT('OENTER STOP VALUE(REAL VALUE): ',$)
       ACCEPT 8015, STOP
       IF(STOP.NE.FLOAT(NUM)) GOTO 8074
       XINC = 1.0
       GOTO 8079
8074
       TYPE 8075
       FORMAT('OINCREMENT OF VARIABLE(REAL VALUE): ',$)
8075
       ACCEPT 8015, XINC
8079
       TYPE 8080
       FORMAT('ODO YOU WANT PLOTTING DATA WRITTEN TO DISK(Y/N)? ',$)
8080
       ACCEPT 8055, ANSWER
       IF(ANSWER.EQ.'N') IFLAG = 1
       TYPE 8085
       FORMAT('OPRINTED DATA WRITTEN TO DISK(Y/N)? ',$)
8085
       ACCEPT 8055, ANSWER
       IF(ANSWER.EQ.'N') IFLAG1 = 1
       TYPE 8090
8090
       FORMAT('OIS ABOVE INPUT DATA CORRECT(Y/N)? ',$)
       ACCEPT 8055, ANS1
       IF(ANS1.EQ.'N') GOTO 8000
       RETURN
       END
```

```
С
  NORMAL: THIS SUBROUTINE NORMALIZES DATA AS OUTLINED.
C
     1. DETERMINE PHASE FROM COMPLEX PRESSURE ARRAY
C
     2. CALCULATE AMPLITUDE FROM MAGNITUDE*COS(PHASE)
С
     3. LOCATE AMPLITUDE AND PHASE MAXIMA AND MINIMA
     4. WRITE RESULTS TO ARRAYS
        SUBROUTINE NORMAL
        COMPLEX PRS(41,41),Z
        Z = PRS(IFIX(CENTER), IFIX(CENTER))
        DO 7005 I = 10,32
        DO 7000 J = 10,32
        IF(PIC(I,J).EQ.'-') GOTO 7000
        PRS(I,J) = PRS(I,J)/Z
        THETA(I,J)=57.295780*ATAN2(AIMAG(PRS(I,J)), REAL(PRS(I,J)))
        AMP(I,J) = COSD(THETA(I,J))
        IF(THETA(I,J).LT.0.0) THETA(I,J) = THETA(I,J) + 360.00
 7005
        CONTINUE
 7000
        CONTINUE
        DO 7025 I = 1, M
        DO 7020 J = 1, M
        IF(PIC(I,J).EQ.'-') GOTO 7020
        IF(AMP(I,J).GT.AMPMAX) AMPMAX = AMP(I,J)
        IF(AMP(I,J).LT.AMPMIN) AMPMIN = AMP(I,J)
        IF(THETA(I,J).GT.THEMAX) THEMAX = THETA(I,J)
        IF(THETA(I,J).LT.THEMIN) THEMIN = THETA(I,J)
        CONTINUE
7020
7025
        CONTINUE
        DAMP = AMPMAX - AMPMIN
        DTHETA = THEMAX - THEMIN
        RPCT(NCOUNT) = PCT
        RPHASE(NCOUNT) = DTHETA
        RAMP(NCOUNT) = DAMP
        RNUM(NCOUNT) = FLOAT(NUM)
        RMAG(NCOUNT) = CABS(Z)
        RIMAG(NCOUNT) = AIMAG(Z)
        RREAL(NCOUNT) = REAL(Z)
        RFREQ(NCOUNT) = FREQ
        RETURN
        END
```

```
RDNAPT: THIS SUBROUTINE RANDOMLY PLACES A POINT SCATTERER WITHIN A
 SURFACE AREA SPECIFIED IN VARIABLE SCTDIM. THE USER VARY APERTURE
       SUBROUTINE RDNAPT
       COMPLEX C, PRS(41,41)
       PCT = FLOAT(NUM)
       SEED1 = .012345
       SEED2 = .543210
       SEED3 = .975310
       SEED4 = .013579
       SCTDIM = .75
       ASFSCT = SCTDIM/(DIM - 1.0)
       SCTRAD = SCTDIM/2.0
       DO 1010 I1 = 1, M
       DO 1005 J1 = 1.M
       XII = FLOAT(II)
       XJ1 = FLOAT(J1)
       TEMP1 = ASF*SQRT((XI1-CENTER)**2 + (XJ1-CENTER)**2)
       IF(TEMP1.GT.TRANR) GOTO 1005
       C = (0.0, 0.0)
       NUMBER = 0
       PIC(I1,J1) = 'X'
       DO 1000 I2 = 1,100000
       SIGN1 = 1.0
       SIGN2 = 1.0
       TEMP5 = RAN(SEED3)
       TEMP6 = RAN(SEED4)
       IF(TEMP5.LT..5000) SIGN1 = -1.0
       IF(TEMP6.LT..5000) SIGN2 = -1.0
       XRAND = SCTDIM * RAN(SEED1) * SIGN1
       YRAND = SCTDIM * RAN(SEED2) * SIGN2
       SEED1 = SEED1 + .13
       SEED2 = SEED2 + .133
       SEED3 = SEED3 + .1333
       SEED4 = SEED4 + .13333
       TEMP3 = XRAND/ASFSCT
       TEMP4 = YRAND/ASFSCT
       TEMP2 = ASFSCT*SQRT((TEMP3+XI1-CENTER)**2 + (TEMP4+XJ1-CENTER)**2)
       IF(TEMP2.GT.SCTRAD) GOTO 1000
       NUMBER = NUMBER + 1
       XLEG2 = SQRT(XRAND**2 + YRAND**2)
       HYPO = SQRT(XLEG2**2 + RANGE**2)
       C = (SCAT/HYPO)*CEXP((0.0,1.0)*XK*(RANGE+HYPO)) + C
       IF(NUMBER.EQ.NUM) GOTO 1004
       CONTINUE
1000
1004
       PRS(I1,J1) = C
1005
       CONTINUE
1010
       CONTINUE
```

RETURN

```
C**********************
  VOLSCT: THIS SUBROUTINE RANDOMLY PLACES A PARTICLE WITHIN A CYLINDER
        SUBROUTINE VOLSCT
        COMPLEX C, PRS(41,41)
       PCT = FLOAT(NUM)
        SEED1 = .012345
        SEED2 = .543210
        SEED3 = .975310
       SEED4 = .013579
       SEED5 = .024531
       DO 2010 II = 10,32
       DO 2005 J1 = 10,32
       TEMP1 = ASF * SQRT((FLOAT(I1)-CENTER)**2+(FLOAT(J1)-CENTER)**2)
       IF(TEMP1.GT.TRANR) GOTO 2005
       NUMBER = 0
       C = (0.0, 0.0)
       PIC(I1,J1) = 'X'
       DO 2000 I2 =1,999999
       SIGN1 = 1.0
       SIGN2 = 1.0
       TEMP5 = RAN(SEED3)
       TEMP6 = RAN(SEED4)
       IF(TEMP5.LT..5000) SIGN1 = -1.0
       IF(TEMP6.LT..5000) SIGN2 = -1.0
       XRAND = APERT * RAN(SEED1) * SIGN1
       YRAND = APERT * RAN(SEED2) * SIGN2
       SEED1 = SEED1 + .13
       SEED2 = SEED2 + .133
       SEED3 = SEED3 + .1333
       SEED4 = SEED4 + .13333
       SEED5 = SEED5 + \cdot 133333
       TEMP3 = XRAND/ASF
       XII = FLOAT(II)
       XJ1 = FLOAT(J1)
       TEMP4 = YRAND/ASF
       TEMP2 = ASF*SQRT((TEMP3+XI1-CENTER)**2+(TEMP4+XJ1-CENTER)**2)
       IF(TEMP2.GT.TRANR) GOTO 2000
       NUMBER = NUMBER + 1
       XLEG2 = SQRT(XRAND**2 + YRAND**2)
       DEPTH = (RAN(SEED5) * .1) + RANGE
       HYPO = SQRT(XLEG2**2 + DEPTH**2)
       C = (SCAT/HYPO)*CEXP((0.0,1.0)*XK*(DEPTH+HYPO)) + C
       IF(NUMBER.EQ.NUM) GOTO 2004
2000
       CONTINUE
2004
       PRS(I1,J1) = C
2005
       CONTINUE
2010
       CONTINUE
       RETURN
```

END

```
C**************
 RDNSCT: THIS SUBROUTINE TAKES THE COORDINATE 11, J1 FROM THE TRANSDUCER
C FACE AND SUMS THE AMPLITUDE AND PHASE DUE TO EACH SCATTERER WITHIN
C THE BEAM PROFILE. ASSUME A PLANAR INCIDENT WAVE WITH A SPHERICAL
С
  REFLECTED WAVEFRONT
C
     1) ASF = ARRAY SCALE FACTOR (CM/#BLOCKS FOR TRANSDUCER)
С
     2) PRS = COMPLEX PRESSURE ARRAY
С
     3) XRAND = RANDOM X COORDINATE (YRAND - Y COORDINATE)
SUBROUTINE RDNSCT
       COMPLEX C, PRS(41,41)
       PCT = FLOAT(NUM)
       SEED1 = .012345
       SEED2 = .543210
       SEED3 = .975310
       SEED4 = .013579
       DO 3010 I1 = 1,M
       DO 3005 J1 = 1, M
       C = (0.0, 0.0)
       NUMBER = 0
       XII = FLOAT(II)
       XJ1 = FLOAT(J1)
       TEMP1 = ASF*SQRT((XI1-CENTER)**2 + (XJ1-CENTER)**2)
       IF(TEMP1.GT.TRANR) GOTO 3005
       PIC(I1,J1) = 'X'
       DO 3000 I2 = 1,10000
       SIGN1 = 1.0
       SIGN2 = 1.0
       TEMP5 = RAN(SEED3)
       TEMP6 = RAN(SEED4)
       IF(TEMP5.LT..5000) SIGN( = -1.0)
       IF(TEMP6.LT..5000) SIGN2 = -1.0
       XRAND = APERT * RAN(SEED1) * SIGN1
       YRAND = APERT * RAN(SEED2) * SIGN2
       SEED1 = SEED1 + .13
       SEED2 = SEED2 + .133
       SEED3 = SEED3 + .1333
       SEED4 = SEED4 + .13333
       TEMP3 = XRAND/ASF
       TEMP4 = YRAND/ASF
       TEMP2 = ASF*SQRT((TEMP3+XI1-CENTER)**2+(TEMP4+XJ1-CENTER)**2)
       IF(TEMP2.GT.TRANR) GOTO 3000
       NUMBER = NUMBER + 1
       XLEG2 = SQRT(XRAND**2 + YRAND**2)
       HYPO = SQRT(XLEG2**2 + RANGE**2)
       C = (SCAT/HYPO)*CEXP((0.0,1.0)*XK*(RANGE+HYPO)) + C
       IF(NUMBER.EQ.NUM) GOTO 3004
 3000
       CONTINUE
 3004
       PRS(I1,J1) = C
 3005
       CONTINUE
 3010
       CONTINUE
```

```
C***********************
  FILINC: INCREMENT DATA FILE NAMES & CALL INFO AND SAVDAT SUBROUTINES
C*****************************
       SUBROUTINE FILINC
       DOUBLE PRECISION FNAME1, FNAME2, FNAME3, FNAME4
C FLAG OPERATIONS:
    0 = PERFORM ROUTINE
     1 = SKIP
       IF(IFLAG.EQ.1.AND.IFLAG1.EQ.1) GOTO 4005
       FNAME1 = 'PLT000.DAT'
       FNAME2 = 'AMPOOO.DAT'
       FNAME3 = 'INFOOO.DAT'
       FNAME4 = 'PHZ000.DAT'
C ALLOW INCREMENT OF FILE NAMES DEPENDING UPON THE CHANGING VARIABLE
       IF(ANS.EQ.'A') ICOUNT = IFIX(APERT * 100.00)
       IF(ANS.EQ.'R') ICOUNT = IFIX(RANGE * 10.00)
       IF(ANS.EQ.'F') ICOUNT = IFIX(FREQ * 10.00)
IF(ANS.EQ.'N') ICOUNT = NUM
       DO 4000 I = 1, ICOUNT
       CALL INCFIL(FNAME1)
       CALL INCFIL(FNAME2)
       CALL INCFIL(FNAME3)
4000
       CALL INCFIL(FNAME4)
       IF(IFLAG.EQ.0) CALL PLTDAT(FNAME1)
       IF(IFLAG1.EQ.O) CALL PRTDAT(FNAME2,FNAME4)
       IF(IFLAG1.EQ.0) CALL INFO(FNAME1, FNAME3)
```

4005 RETURN END

SUBROUTINE INCVAR

IFLAG2 = 0

IF(ANS.NE.'N') GOTO 5000
NUM = NUM + IFIX(XINC)
ISTOP = IFIX(STOP)
IF(NUM.GT.ISTOP) IFLAG2 = 1
GOTO 5015

- 5000 IF(ANS.EQ.'A'.OR.ANS.EQ.'F') GOTO 5005

 RANGE = RANGE + XINC

 IF(RANGE.GT.STOP) IFLAG2 = 1

 GOTO 5015
- 5005 IF(ANS.EQ.'F') GOTO 5010 APERT = APERT + XINC IF(APERT.GT.STOP) IFLAG2 = 1 GOTO 5015
- 5010 FREQ = FREQ + XINC IF(FREQ.GT.STOP) IFLAG2 = 1
- 5015 RETURN END

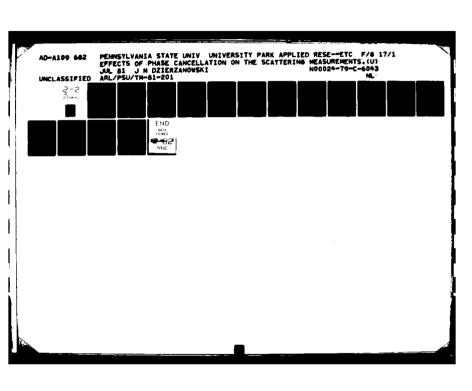
```
C*********************
  LINSCT: THIS SUBROUTINE TAKES EACH COORDINATE ON THE TRANSDUCER
  AND SUMS THE AMPLITUDE AND PHASE DISTRIBUTION DUE TO EACH SCATTER.
  THE SCATTERERS ARE ARRANGED IN A LINEAR (ONE-DIMENSIONAL) ARRAY.
       SUBROUTINE LINSCT
       COMPLEX C, PRS(41,41)
       XEDGE = IFIX(CENTER) - INT(DIM/2.0)
       YEDGE = CENTER
       PCT = FLOAT(NUM)
       DO 6020 I =1,M
       DO 6015 J = 1.M
       XI = FLOAT(I)
       XJ = FLOAT(J)
       XTEMP = ASF*SQRT((XI-CENTER)**2 + (XJ-CENTER)**2)
       IF(XTEMP.GT.TRANR) GOTO 6015
       C = (0.0, 0.0)
       PIC(I,J) = 'X'
       IF(NUM.NE.1) GOTO 6000
       XLEG2 = SQRT((((ASF)*(XI-XEDGE)-(TRANR))**2) +
       1 (((XJ-YEDGE)*(ASF))**2))
       HYPO = SQRT(XLEG2**2 + RANGE**2)
       C = (SCAT/HYPO)*CEXP((0.0,1.0) *XK*(RANGE+HYPO))
       GOTO 6011
6000
       DO 6010 I2 =1, NUM
       XI2 = FLOAT(I2)
       XLEG2 = SQRT(((ASF)*(XI-XEDGE)-(XI2-1.0)*(PSF))**2 +
       1 ((XJ-YEDGE)*(ASF))**2)
       HYPO = SQRT(XLEG2**2 + RANGE**2)
       C = (SCAT/HYPO)*CEXP((0.0,1.0) * XK * (RANGE+HYPO)) + C
6010
       CONTINUE
6011
       PRS(I,J) = C
6015
       CONTINUE
6020
       CONTINUE
       RETURN
```

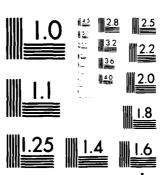
END

```
C************************
C PARCNT: LOADS PARTICLE COUNT ARRAY (RPCT) USED IN THE RECTANGULAR
  SCATTERERING ARRANGEMENT IN THE NUMBER COUNT ARRAY (RNUM) FOR USE IN
  SAVDAT SUBROUTINE.
SUBROUTINE PARCNT
C SCTANS:
С
    L,R,V,A = EXIT
C
          = PERFORM TRANSFER
      T = SCTANS
      IF(T.EQ.'L'.OR.T.EQ.'R'.OR.T.EQ.'V'.OR.T.EQ.'A') GOTO 7010
      DO 7000 I = 1, NCOUNT
      RNUM(I) = RPCT(I)
7000
      CONTINUE
      TYPE 7005
7005
      FORMAT('ODATA TRANSFER FROM RPCT ARRAY TO RNUM COMPLETED!')
7010
      RETURN
      END
C**********************
C DECIDE: THIS SUBROUTINE CALLS THE CORRECT SCATTERERING ROUTINE BASED
  ON USER INPUT.
C*********************************
      SUBROUTINE DECIDE
C SCATTERER ROUTINE: USER DEFINED
   L = LINEAR ARRAY
С
   O = RECTANGULAR ARRAY
С
   R = RANDOM ARRAY
С
   V = RANDOM VOLUME
    A = RANDOM ARRAY CONSTANT SCATTERING APERTURE
      IF(SCTANS.EQ.'L') CALL LINSCT
      IF(SCTANS.EQ.'O') CALL RCTSCT
      IF(SCTANS.EQ.'R') CALL RDNSCT
      IF(SCTANS.EQ.'V') CALL VOLSCT
      IF(SCTANS.EQ.'A') CALL RDNAPT
      RETURN
      END
```

```
C**********************************
С
C
  RCTSCT: BACKSCATTER ROUTINE FEATURING A RECTANGULAR ARANGEMENT
  OF PARTICLES WITHIN A TRANSDUCER BEAM PROFILE
SUBROUTINE RCTSCT
       COMPLEX C, PRS(41,41)
       XEDGE = 10.0
       YEDGE = 10.0
       TEMP5 = FLOAT(NUM)/2.0
       TEMP2 = TEMP5 - INT(TEMP5)
       IF(TEMP2.NE.0.00) GOTO 3000
       PCNTR = TEMP5 + .5000
       GOTO 3005
 3000
       PCNTR = INT(TEMP5) + 1.0
 3005
       DO 3025 I1 = 10,32
       DO 3020 J1 = 10.32
       XII = FLOAT(II)
       XJ1 = FLOAT(J1)
       TEMP1 = ASF*SQRT((XI1-CENTER)**2 + (XJ1-CENTER)**2)
       IF(TEMP1.GT.TRANR) GOTO 3020
       C = (0.0, 0.0)
       PIC(II,JI) = 'X'
       DO 3015 I2 = 1,NUM
       DO 3010 J2 = 1, NUM
       TEMP3=PSF*SQRT((FLOAT(I2)-PCNTR)**2+(FLOAT(J2)-PCNTR)**2)
       IF(TEMP3.GT.TRANR) GOTO 3010
       XLEG2=SQRT(((ASF)*(XI1-XEDGE)-(FLOAT(I2)-1.0)*(PSF))**2 +
       1 ((XJ1-YEDGE)*(ASF)-(FLOAT(J2)-1.0)*(PSF))**2)
       HYPO = SQRT(XLEG2**2 + RANGE**2)
       C = (SCAT/HYPO)*CEXP((0.0,1.0)*XK*(RANGE+HYPO)) + C
       IF(XJ1.NE.CENTER.OR.XII.NE.CENTER) GOTO 3010
       IF(I2.NE.IFIX(PCNTR).OR.J2.NE.IFIX(PCNTR)) GOTO 3010
       PCT = 0.0
       DO 3007 I3 = 1, NUM
       DO 3006 J3 = 1,NUM
       TEMP4=PSF*SQRT((FLOAT(I3)-PCNTR)**2 + (FLOAT(J3)-PCNTR)**2)
       IF(TEMP4.LE.TRANR) PCT = PCT + 1
 3006
       CONTINUE
 3007
       CONTINUE
 3010
       CONTINUE
 3015
       CONTINUE
       PRS(I1,J1) = C
 3020
       CONTINUE
 3025
       CONTINUE
       RETURN
       END
```

```
C
C WARN: CHECK PARAMETERS TO SEE IF DATA ASSUMPTIONS HOLD
SUBROUTINE WARN
4003
     XKA = XK * PARRAD * 1.0E-04
      IF(XKA.GT.1.0) TYPE 4005
4005
     FORMAT('***KA > 1.0 CHECK INITIAL CONDITIONS***')
      IF(RANGE.LT.XNEAR) TYPE 4010
4010
     FORMAT('0***SCATTERERING ARRAY WITHIN NEARFIELD***')
     RETURN
     END
C************************
C VOLDAT: WRITE AVERAGE RECEIVED PRESSURE PER VOLUME TO DISK
SUBROUTINE VOLDAT
      DOUBLE PRECISION FNAME
      IF(SCTANS.NE.'V') GOTO 5015
     FNAME = 'VD000.DAT'
      ICOUNT = IFIX(APERT * 100.00)
     DO 5000 I =1, ICOUNT
5000
     CALL INCFIL(FNAME)
     CALL OPEN(21, 'FILE', FNAME)
      DO 5005 I =1, NCOUNT
     WRITE(21,5010) RNUM(I), RVOL(I)
5005
     CONTINUE
5010
     FORMAT(1X,F11.6,1X,F11.6)
     CALL CLOSE(21)
     RETURN
5015
      END
```





MICROCOPY RESOLUTION TEST CHART NATIONAL BUREAU OF STANLARI SPACE

```
С
  ASKFEW: THIS SUBROUTINE IS USED WHEN A MACRO FILE CONTROLS EXECUTION
C******************************
       SUBROUTINE ASKFEW
       ACCEPT 8000, NUM
8000
       FORMAT(I)
8005
       FORMAT(F)
       XINC = 1.0
       STOP = 100.0
       APERT = .25
       FREQ = 5.0
       RANGE = 15.0
       IFLAG1 = 0
       ANS = 'N'
       IFLAG = 1
       SCTANS = 'V'
       RETURN
       END
C**********************
  APPSTR: APPENDS ONE CHARACTER STRING TO ANOTHER
    1) STRING - STRING TO BE EXTENDED
C
             - NUMBER OF CHARACTERS IN STRING UPON ENTRY
C
    3) ADDTN - STRING TO BE APPENDED
C
             - NUMBER OF CHARACTERS TO BE APPENDED
    4) NADD
C
    5) 167
             - CHARACTER TYPE : 6 = 6-BIT (FROM ASCPK)
C
                                7 = 7 - BIT (STD. ASCII)
C***********************
       SUBROUTINE APPSTR(STRING, NCH, ADDTN, NADD, 167)
       DIMENSION STRING(1)
       NBWD = (36/167) * 167
       NBITS = NCH * 167
       NWD = NBITS/NBWD
       NBITR = NBITS - NWD * NBWD - 1
       NWD = NWD + 1
       CALL BPOINT(167, STRING(NWD), NBITR, BPS)
       CALL BPOINT(167, ADDTN, -1, BPA)
       DO 9000 I =1, NADD
       CALL ILDB(ICH, BPA)
       CALL IDPB(ICH, BPS)
       CONTINUE
9000
       RETURN
       END
```

```
STAT: CALCULATE USING AMP(I,J) AND THETA(I,J) ARRAYS STATISTICAL
C
         PARAMETERS - MEAN AND VARIANCE.
C
C************************
       SUBROUTINE STAT
       K = 0
       TEMPA = 0.0
       TEMPB = 0.0
       DO 1005 I = 1, M
               DO 1000 J = 1,M
               IF(PIC(1,J).EQ.'-') GOTO 1000
               TEMPA = TEMPA + AMP(I,J)
               TEMPB = TEMPB + THETA(I,J)
               K = K + 1
 1000
       CONTINUE
 1005
       CONTINUE
       AMEAN = TEMPA/FLOAT(K)
       PMEAN = TEMPB/FLOAT(K)
       K = 0
       TEMPA = 0.0
       TEMPB = 0.0
       DO 1015 I = 1,M
               DO 1010 J = 1, M
               IF(PIC(I,J).EQ.'-') GOTO 1010
               TEMPA = TEMPA + (AMP(I,J) - AMEAN)**2
               TEMPB = TEMPB + (THETA(I,J) - PMEAN)**2
C
               K = K + 1
 1010
       CONTINUE
 1015
       CONTINUE
       AVAR = TEMPA/(FLOAT(K) - 1.0)
       PVAR = TEMPB/(FLOAT(K) - 1.0)
       TYPE 1020, AMEAN, PMEAN
       FORMAT('OMEAN AMPLITUDE = ',F11.6,' MEAN PHASE = ',F11.6)
 1020
       TYPE 1025, AVAR
 1025
       FORMAT('OAMP VARIANCE = ',F11.6)
        RETURN
```

END

SUBROUTINE NAME(FNAME5, FNAME6)
DOUBLE PRECISION F1, FNAME5, FNAME6, S2

A2 = ANS S2 = SCTANS F1 = '0000.DAT' FNAME6 = 'TAB000.DAT'

INAME = IFIX(APERT * 100.00)

CALL APPSTR(S2,1,A2,1,7) CALL APPSTR(S2,2,F1,4,7)

FNAME5 = S2

DO 2000 I = 1, INAME CALL INCFIL(FNAME5) CALL INCFIL(FNAME6)

2000 CONTINUE

RETURN END

PLT3D

The graphics program, PLT3D, plots the three-dimensional amplitude and phase distributions across a transducer aperture. This program can be executed at installations supporting the TOPS-10 operating system and Tektronix AG-II graphics software. PLT3D operates in an interactive mode allowing flexible control of graphics parameters and subsequent plot generation. The main graphics subroutine, VISDO (Visualize Double Surfaces), requires data to be expressed in cartesian coordinates. VISDO plots an array of M x N elements, each array element having a distinct value. The user specifies the shear or rotation, relative elevation and span of the plot. The user may also specify the plot not to be cross-hatched, by including the subroutine TSPLT, meaning only lines in the left-to-right direction are drawn rather than left-to-right and front-to-back. The algorithm used by TSPLT accounts for hidden lines thus maintaining data integrity.

CPLOT

The FORTRAN program CPLOT constructs contour plots using data generated by PHASE. Once the amplitude and phase data have been read into program arrays, the number of contour levels must be specified. This parameter is used to determine how many contours of equivalue are drawn between the maximum and minimum data points. The contour subroutine PLTKP then drawn the final plot. This plot only shows the regularity of the data in one plane with no evidence of relative height between contours.

```
C*********************
  PHASE-CANCELLATION STUDIES: 3D PLOTTING PROGRAM
  THIS PROGRAM USES DATA FILES CREATED BY PHASE.F4 AND CONSTRUCTS
  3-D PLOTS. THE PROGRAM REQUESTS U AND V SHEAR DIRECTIONS
C EAST OR WEST ORIENTATION AND HAS FLEXIBLE CONTROL OVER SCALE
C AND COMPRESSION FACTORS.
C RUN COMMAND: PLT3D.F4, NUMBER.REL, @SYS:GRA3D, @SYS:GRALIB
C***********************
       DOUBLE PRECISION FNAME!
       DIMENSION AMP(41,41), THETA(41,41)
       EXTERNAL PLTCA
       TYPE 1001
                     1)
 1001
       FORMAT('0
       TYPE 1002
       TYPE 1001
 1000
       TYPE 1005
       FORMAT(20X, 'BIOENCINEERING: 3-D GRAPHICS PROGRAM')
 1002
 1005
       FORMAT('OENTER DATA FILE NAME: ',$)
       ACCEPT 1010, FNAME1
 1010
       FORMAT(A10)
C READ IN DATA FILE CREATED BY PHASE.F4
       CALL OPEN(21, 'FILE', FNAME1)
       READ(21,1025) M, AMPMIN, AMPMAX, THEMIN, THEMAX, SCTANS
 1025
       FORMAT(13,1X,F11.5,1X,F11.5,1X,F11.5,1X,F11.5,1X,A1)
       READ(21,1026) NUM, TRANR, RANGE, FREQ, APERT, PCT
 1026
       FORMAT(15,1X,F11.5,1X,F11.5,1X,F11.5,1X,F11.5)
       READ(21,1027)((AMP(I,J),J=1,M),I=1,M)
       READ(21,1027)((THETA(I,J),J=1,M),I=1,M)
 1027
       FORMAT(41(F11.6,1X))
       CALL CLOSE(21)
       CALL BELL
C MULTIPLY AMPLITUDE AND PHASE DATA BY XSIGN TO ACCOUNT FOR PLOTTING
C BY SUBROUTINE VISDO
       XSIGN = -1.0
       DO 1039 I = 1, M
       DO 1038 J = 1.M
       AMP(I,J) = XSIGN * AMP(I,J)
 1038
       THETA(I,J) = XSIGN * THETA(I,J)
 1039
       CONTINUE
```

```
C PROMPT USER FOR PLOTTING NAME AND SCALE FACTORS TO BE USED BY VISDO
1040
        TYPE 1045
        FORMAT('OENTER PLOT NAME (5 CHARACTERS): ',$)
1045
        ACCEPT 1050, PNAME
 1050
        FORMAT(A5)
        TYPE 1055
        FORMAT('OEAST/WEST VIEW (EAST = -1, WEST = +1): ',$)
 1055
        ACCEPT 1060, LVIEW
 1060
        FORMAT(I)
        TYPE 1065
        FORMAT('OENTER U SHEAR (REAL 0.0 TO 1.0): ',$)
 1065
        ACCEPT 1070, USHEAR
 1070
        FORMAT(F)
        TYPE 1075
1075
        FORMAT('OENTER V SHEAR (REAL 0.0 - 1.0): ',$)
        ACCEPT 1070, VSHEAR
        TYPE 1080
1080
        FORMAT('OENTER COMPRESSION FACTOR: ',$)
        ACCEPT 1070, COMP
        TYPE 1085
 1035
        FORMAT('OENTER SPAN COMPRESSION FACTOR: ',$)
        ACCEPT 1070, SFACTR
        ASPAN1 = 1.0 * COMP
        ASPAN2 = -ASPAN1
        ASPAN1 = ASPAN1/SFACTR
        TSPAN1 = (THEMAX - THEMIN)*COMP
        TSPAN2 = -TSPAN1
        TSPAN2 = TSPAN2/SFACTR
1141
        TYPE 1145
1145
        FORMAT('ODO YOU WISH TO PLOT AMPLITUDE OR PHASE (A/P): ',$)
        ACCEPT 1150, ANS
        IF(ANS.NE.'A'.AND.ANS.NE.'P') GOTO 1141
C SET UP GRAPHIC LIBRARY AND CALL PLOTTING ROUTINES
        CALL PLT00
        CALL BELL
        CALL FRAME
        CALL PRT(ANS, PCT, TRANR, RANGE, FREQ, SCTANS)
        CALL PLTLA(PNAME)
1150
        FORMAT(A1)
        IF(ANS.EQ.'P') GOTO 1155
        CALL VISDO(ASPAN1, AMP, AMP, ASPAN2, M, M, M, M, USHEAR, VSHEAR,
        1 LVIEW,-1,PLTCA)
        GOTO 1160
1155
        CALL VISDO(TSPANI, THETA, THETA, TSPAN2, M, M, M, M, USHEAR, VSHEAR,
        1 LVIEW,-1,PLTCA)
 1160
        CONTINUE
        CALL BELL
        STOP
        END
```

```
C*********************
   PRT: PRINT NUMERICAL INFORMATION ON GRAPH
        SUBROUTINE PRT(ANS, PCT, TRANR, RANGE, FREQ, SCTANS)
        DIMENSION A(6), B(5), C(5), D(2), E(2), F(3), G(4), H(3), I(3)
        DATA(A(K), K=1,6)/'NORMALIZED RECEIVED AMPLITUDE'/
        DATA(B(K), K=1,5)/'NORMALIZED RECEIVED PHASE'/
        DATA(D(K), K=1,2)/'APERTURE:'/
        DATA(E(K), K=1,2)/'DISTANCE:'/
        DATA(F(K), K=1,3)/'RANDOM ARRAY'/
        DATA(G(K), K=1,4)/'RECTANGULAR ARRAY'/
        DATA(H(K),K=1,3)/'LINEAR ARRAY'/
        DATA(I(K), K=1,3)/'RANDOM VOLUME'/
        APERT =TRANR * 2.0
        CALL CHRSET(21,33)
        IF(ANS.EQ.'P') GOTO 2000
        CALL JUSTFX(30,A,0,LEN,IOFS)
        CALL MOVABS(512+IOFS,725)
        CALL ANCHOS(A, LEN)
        GOTO 2005
 2000
        CALL JUSTFX(25, B, 0, LEN, IOFS)
        CALL MOVABS(512+IOFS,725)
        CALL ANCHOS(B, LEN)
 2005
        CALL CHRSET(14,22)
        CALL MOVABS(100,655)
        STR ='NUM:'
        NUM = IFIX(PCT)
        CALL ANCHOS(STR,4)
        CALL NUMBER(NUM, '15')
        CALL MOVABS(100,630)
        STRING = 'CM'
        CALL JUSTFX(10,D,-1,LEN,IOFS)
        CALL ANCHOS(D, LEN)
        CALL NUMBER(APERT, 'F6.2')
        CALL ANCHOS(STRING, 2)
        CALL MOVABS(100,605)
        CALL ANCHOS(E,9)
        CALL NUMBER(RANGE, 'F7.2')
        CALL ANCHOS(STRING, 2)
        CALL MOVABS(100,580)
        STR = FREQ:
        CALL ANCHOS(STR,5)
        CALL NUMBER(FREQ, 'F5.2')
        STR = 'MHZ'
        CALL ANCHOS(STR,3)
        CALL MOVABS(100,555)
        IF(SCTANS.EQ.'R'.OR.SCTANS.EQ.'L'.OR.SCTANS.EQ.'V') GOTO 2010
        CALL JUSTFX(17,G,-1,LEN,IOFS)
        CALL ANCHOS(G, LEN)
        GOTO 2030
```

```
2010
       IF(SCTANS.EQ.'R'.OR.SCTANS.EQ.'V') GOTO 2020
       CALL JUSTFX(12, H,-1, LEN, IOFS)
       CALL ANCHOS(H, LEN)
       GOTO 2030
       IF(SCTANS.EQ.'R') GOTO 2025
2020
       CALL JUSTFX(13, I,-1, LEN, IOFS)
       CALL ANCHOS(I, LEN)
       GOTO 2030
2025
       CALL JUSTFX(12, F, -1, LEN, IOFS)
       CALL ANCHOS(F, LEN)
2030
       RETURN
       END
```

SUBROUTINE FRAME
CALL PLOT(0.0,0.0,3)
CALL PLOT(0.0,11.0,2)
CALL PLOT(3.5,11.0,1)
CALL PLOT(8.5,0.0,1)
CALL PLOT(0.0,0.0,1)
CALL PLOT(4.25,5.50,-3)
RETURN
END

```
С
С
  TSPLT: PLOT 3-D REPRESENTATION ON DATA WITHOUT CROSSHATCHING
C
     U(K) - ARRAY FOR DISTANCE ALONG X COORDINATE
C
     V(K) - ARRAY CONTAINING AMPLITUDE AT DISTANCE X
C
     IX(J,I) - CONVERTS 2 DIMENSIONAL ARRAY INTO 1
C
C**********************
       SUBROUTINE TSPLT(ASPAN1, AMP, ASPAN2, N, M, USHEAR, VSHEAR, LV)
       EXTERNAL PLTCA
       DIMENSION AMP(1), U(501), V(501)
C FUNCTION STATEMENTS & CALL NULL INITIAL HORIZON FOR HIDDEN LINE
       IX(J,I) = (I-1) * M + J
       AM(J,I) = ZS * (AMP(IX(J,I)) - ASPAN1)
       CALL VISNH
C SET UP SCALE FACTORS USING SHEAR VALUES
       MK = 501
       ZS = (1.0 - VSHEAR)/(ASPAN2 - ASPAN1)
       DELTAU = USHEAR/FLOAT(M - 1)
       DELTAV = VSHEAR/FLOAT(M - 1)
       DELTAS = (1.0 - USHEAR)/FLOAT(M - 1)
       VE = 0.0
C SET UP DATA FOR VISUALIZE HORIZON ROUTINE VISHO
       DO 1010 I = 1,M
          K = 0
          EU = USHEAR - (DELTAU * FLOAT(I))
          DO 1000 J = 1,M
            K = MINO(K+1,MK)
            U(K) = EU
            V(K) = VE + AM(J,I)
            EU = EU + DELTAS
 1000
          CONTINUE
          CALL VISHO(U,V,K,1,PLTCA)
          CALL VISHO(U,V,K,-1,PLTCA)
          VE = VE + DELTAV
 1010
       CONTINUE
       RETURN
       END
```

```
PHASE-CANCELLATION STUDIES: CONTOUR PLOTTING PROGRAM
С
C THIS PROGRAM USES DATA CREATED FROM PHASE.F4 AND PLOTS USER
  SPECIFIABLE CONTOUR INTERVALS. USES 3DPLOT.F4 AS THE MAIN ROUTINE.
  LOAD CPLOT.F4,@SYS:GRA3D
C**********************
       DOUBLE PRECISION FNAME!
       DIMENSION AMP(41,41), THETA(41,41)
       EXTERNAL PLTCA
       TYPE 1001
       TYPE 1005
 1000
       FORMAT(20X, 'BIOENGINEERING: CONTOUR GRAPHICS PROGRAM')
 1001
       FORMAT('OPLEASE ENTER PLOTTING DATA FILE: ',$)
 1005
       ACCEPT 1010, FNAME1
       FORMAT(A10)
 1010
C READ IN DATA FILE AS SPECIFIED BY USER
       CALL OPEN(21, 'FILE', FNAME1)
       READ(21.1015) M, AMPMIN, AMPMAX, THEMIN, THEMAX, SCTANS
 1015
       FORMAT(13,1X,F11.5,1X,F11.5,1X,F11.5,1X,F11.5,1X,A1)
       READ(21,1020) NUM, TRANR, RANGE, FREQ, APERT, PCT
       FORMAT(15,1X,F11.5,1X,F11.5,1X,F11.5,1X,F11.5)
 1020
       READ(21,1025)((AMP(I,J),J=i,M),I=i,M)
        READ(21,1025)((THETA(I,J),J=1,M),I=1,M)
 1025
       FORMAT(41(F11.6,1X))
       CALL CLOSE(21)
C SET UP PLOTTING PARAMETERS
 1050
       CINT1 = AMPMIN
       CINT2 = AMPMAX
       NUMX = M
        NUMY = M
       SUBX = 5.0
       SUBY = 5.0
       TYPE 1055
 1055
       FORMAT('OENTER PLOT NAME (MAX 5 CHARACTERS): ',$)
       ACCEPT 1060, FILNAM
 1060
       FORMAT(A5)
       TYPE 1065
        FORMAT('OHOW MANY CONTOUR LEVELS (INTEGER): ',$)
 1065
        ACCEPT 1070, NLEVELS
 1070
       FORMAT(I)
C CALL GRAPHICS LIBRARY ROUTINES AND CALL CONTOUR ROUTINE PLTKP
        CALL PLT00
```

CALL PLTFR

CALL PLTLA(FILNAM)

CALL PLTKP(CINT1, AMP, CINT2, NLEVEL, SUBX, M, SUBY, M, PLTCA)

CALL BELL

TYPE 1035

FORMAT('OREPEAT(Y/N): ',\$) 1035

ACCEPT 1080, ANS IF(ANS.EQ.'Y') GOTO 1050

STOP

END

BATGEN

BATGEN is a FORTRAN program written to control the batch stream of the PDP-10 at the Hybrid Computer Laboratory. The program reads a parameter data file after each successful execution of PHASE. BATGEN then writes a new batch control file and resubmits PHASE to the batch controller for execution. The parameter data file, named PARAM.DAT, contains input values of aperture, frequency, range, and the number of scatterers. This file may also contain start, stop, and increment values if the user is changing one of the above parameters. The user must ensure that disk memory allocation is not exceeded when using the batch controller or program execution will fail.

```
BATCH CONTROL FILE GENERATOR - BATGEN.F4
С
C
C PROGRAM DESCRIPTION: PARAM.DAT CONTAINS THE 8 INPUTS TO PHASE.F4
C WHEN USING THE ASKFEW SUBROUTINE. THE PROGRAM READS IN THE DATA
C FILE AND REWRITES IT TO A CONTROL FILE NAMED RDN.CTL FOR BATCH USE.
C***********************
        REAL PARAM(10.8)
        CALL OPEN(21, 'FILE', 'PARAM.DAT')
        ILINE = 1
        READ(21,1005,END=1010)(PARAM(ILINE,J),J=1,8)
 1000
 1005
        FORMAT(8F)
        ILINE = ILINE + 1
        GOTO 1000
 1010
        CLOSE(UNIT=21, DISPOSE='DELETE')
C NOW THAT THE DATA FILE HAS BEEN LOADED INTO PARAM ARRAY, CHECK
C LAST OPERATION, REWRITE DATA BACK TO DISK OMITTING FIRST LINE
        NLINE = ILINE - 1
        IF(NLINE.EQ.1) GOTO 1025
        CALL OPEN(21, 'FILE', 'PARAM.DAT')
        DO 1020 ILINE =2, NLINE
        WRITE(21,1015)(PARAM(ILINE,J),J=1,8)
 1015
        FORMAT(3F10.5)
 1020
        CONTINUE
        CALL CLOSE(21)
C WRITE BATCH CONTROL FILE, CHANGE LOCATION 1 & 5 IN PARAM ARRAY TO
 INTEGER VARIABLES FOR INPUT TO ASKFEW SUBROUTINE
        CALL OPEN(21, 'FILE', 'RDN.CTL')
 1025
        IPAR1 = PARAM(1,1)
        IPAR5 = PARAM(1,5)
        WRITE(21,1030) IPAR1, PARAM(1,2), PARAM(1,3), PARAM(1,4),
                IPAR5, PARAM(1,6), PARAM(1,7), PARAM(1,8)
        FORMAT('.SET TIME 0',/,

'.SET HPQ 0',/,'.SET DSKPRI 0',/,'.RUN PHASE'/

'*',I/,'*',F/,'*',F/,'*','

'*',I/,'*',F/,'*',F/,'*',F/,'*N')
 1030
        IF(NLINE.EQ.1) COTO 1100
        WRITE(21,1035)
 1035
        FORMAT('.RUN BATGEN'/,
                 '.SUBMIT RDN.CTL/RESTARTABLE/UNIQUE:0')
 0011
        CALL CLOSE(21)
        STOP
        END
```

```
C***********
  PHASE-CANCELLATION STUDIES: BIOENGINEERING
  CALCULATE HISTOGRAM OF AVERAGE RECEIVED PRESSURE DATA FOR A
  RANDOM PLANAR DISTRIBUTION OF SCATTERERS
C****************
       DIMENSION AMP(41,41), THETA(41,41), PIC(41,41), AVGDAT(1/300)
       COMPLEX PRS(41.41).C
 INPUT VARIABLES AND INTIALIZE ULTRASONIC PARAMETERS
       TYPE 100
 100
       FORMAT('OPLEASE ENTER RANGE, APERT, NUM: ',$)
       ACCEPT 105, RANGE, APERT, NUM
 105
       FORMAT(F,F,I)
       FREQ = 5.00
       M = 41
       DIM = 23.0
       SCAT = 1.0
       VELCTY = 1500.00
       WAVEL = (VELCTY/(FREQ*1.0E03))
       XK = (2.0 * 3.14159)/(WAVEL/10.0)
       CENTER = INT(M/2.0) + 1.0
       TRANR = APERT/2.0
       ASF = (APERT/(DIM-1.00))
       DO 1005 I = 1, M
       DO 1000 J = 1,M
 1000
       PIC(I,J) = '-'
1005
       CONTINUE
C DETERMINE PARTICLE LOCATION IN UNITS OF BLOCKS AND SEE IF WITHIN BEAM
C THEN SEARCH TRANSDUCER COORDINATES - CHECK IT WITHIN BEAM ALSO -
C CALCULATE THE DISTANCE BETWEEN THE TWO SETS OF COORDINATES AND CONVERT
 CENTIMETERS - USE THIS VALUE IN THE GEOMETRY
       DO 1045 I = 1,NUM
1010
       SEED1 = SEED1 + .131
       SEED2 = SEED2 + .1331
       XCOOR = RAN(SEED1) * FLOAT(M)
       YCOOR = RAN(SEED2) * FLOAT(M)
       TEMP1 = ASF * SQRT((XCOOR-CENTER)**2 + (YCOOR-CENTER)**2)
       IF(TEMP1.GT.TRANR) COTO 1010
               DO 1020 \text{ I1} = 1,M
               DO 1015 J1 = 1,M
               T=ASF*((I1-CENTER)**2 + (J1-CENTER)**2)
               IF(T.GT.TRANR) GOTO 1015
               PIC(I1,J1) = 'X'
               DIST=ASF*SQRT((XCOOR-I1)**2 + (YCOOR-J1)**2)
               HYPO=SQRT(DIST**2 + RANGE**2)
               PRS(I1,J1)=(SCAT/HYPO)*CEXP((0.0,1.0)*XK*(RANGE+HYPO))
 1015
       CONTINUE
 1020
       CONTINUE
```

```
C LOCATE CENTER VALUE OF THE PRESSURE ARRAY AND ASSIGN TO C FOR
C NORMALIZATION OF THE PRESSURE VALUES - CALCULATE THE AMPLITUDE AND
  PHASE VALUES AT EACH LOCATION ON THE TRANSDUCER SURFACE AREA
       .C = PRS(IFIX(CENTER), IFIX(CENTER))
        DO 1030 \text{ II} = 10.32
        DO 1025 \text{ JJ} = 10,32
                IF(PIC(II,JJ).EQ.'-') GOTO 1025
                PRS(II,JJ) = PRS(II,JJ)/C
                 THETA(II,JJ)=57.29580*ATAN2(AIMAG(PRS(II,JJ)),
                REAL(PRS(II,JJ)))
                AMP(II,JJ) = COSD(THETA(II,JJ))
 1025
        CONTINUE
 1030
        CONTINUE
        K = 0
        TEMP = 0.0
        DO 1040 \text{ II} = 10.32
        DO 1035 JJ = 10,32
                IF(PIC(II,JJ).EQ.'-') GOTO 1035
                TEMP = TEMP + AMP(II,JJ)
                K = K + 1
 1035
        CONTINUE
 1040
        CONTINUE
        AVGDAT(I) = TEMP/FLOAT(K)
 1045
        CONTINUE
C END NUMBER LOOP AND CALCULATE MEAN AND VARIANCE OF AVGDAT ARRAY
        K = 0
        TEMP = 0.0
        DO 1050 I = 1, NUM
                TEMP = TEMP + AVGDAT(I)
                K = K + 1
 1050
        CONTINUE
        AMEAN = TEMP/FLOAT(K)
        TEMP = 0.0
        DO 1055 I =1,NUM
                TEMP = TEMP + (AVGDAT(I)-AMEAN)**2
 1055
        CONTINUE
        AVAR = TEMP/(FLOAT(K)-1.0)
  WRITE RESULTS TO DISK IN FILE SUM.DAT
        CALL OPEN(21, 'FILE', 'SUM.DAT')
        WRITE(21,1060) AMEAN, AVAR
        FORMAT(5X, 'MEAN=', F11.7, 'VARIANCE =', F11.7, //)
 1060
        WRITE(21,1061) RANGE, APERT, NUM
 1061
        FORMAT(5x, 'RANGE = ',F7.2,' APERTURE = ',F6.2,' NUM = ',13,//)
        DO 1070 I =1, NUM
        WRITE(21,1065) I,AVGDAT(I)
 1065
        FORMAT(5x, 13, 3x, F11.5)
 1070
        CONTINUE
        CALL CLOSE(21)
        STOP
        END
```

DISTRIBUTION LIST FOR TM 81-201

Commander (NSEA 0342) Naval Sea Systems Command Department of the Navy Washington, DC 20362

Copies 1 and 2

Commander (NSEA 9961) Naval Sea Systems Command Department of the Navy Washington, DC 20362

Copies 3 and 4

Defense Technical Information Center 5010 Duke Street Cameron Station Alexandria, VA 22314

Copies 5 through 10

